
Subject Index

When the page number of an index entry refers to a definition, then the page number is in italics. When the index entry appears in a footnote, then the letter “n” is appended to the page number. A page range for a topic indicates that either the topic is discussed in the given page range or that each page in the range mentions the topic.

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