Announcements

- Enrollment
 - Now 1 on the waitlist
- Reading
 - Chapter 3 (3.3-3.6)
- Project #2
 - Handout is on the web
 - Due on Monday Sept 24th (10 AM)
 - Reminder, no credit for late work

Error Codes (cont.)

Error Recovery

- Given m bits of data and r bits of error code
- Want to correct any one bit error
- There are n words one bit from each valid message
 - so need n+1 words for each valid message
 - thus $(n + 1) 2^m <= 2^n$
 - but n = m + r so $(m + r + 1) <= 2^r$

Hamming Code

- recovers from any one bit error
- number bits from left (starting at 1)
 - power of two bits are parity
 - rest contain data
- bit is checked by all parity bits in its sum of power expansion
 - bit 11 is used to compute parity bits 1, 2, and 8

Hamming Code Example

Char	ASCII	Hamming
Н	1001 000	0011 0010 000
a	1100 001	1011 1001 001
m	1101 101	1110 1010 101
	1101 001	0110 1011 001

Burst Errors

- can send hamming codes by column rather than row
- if use k rows, then can detect any burst error up to k bits
 - uses kr bits to check a block km bits long

Computing a Hamming Code

Bit #s	1	2	3	4	5	6	7	8	9	10	11
Parity/Data	Р	Р	D	Р	D	D	D	Р	D	D	D
Data To Snd			1		0	0	1		0	0	0
Parity Bit 1	0		1		0		1		0		0
Parity Bit 2		0	1			0	1			0	0
Parity Bit 4				1	0	0	1				
Parity Bit 8								0	0	0	0
Message	0	0	1	1	0	0	1	0	0	0	0

Checking & Correcting a Hamming Code

Bit #s	1	2	3	4	5	6	7	8	9	10	11
Parity/Data	Р	Р	D	Р	D	D	D	Р	D	D	D
Data Sent	0	0	1	1	0	0	1	0	0	0	0
Data Recv	0	0	0	1	0	0	1	0	0	0	0
Parity Bit 1	1		0		0		1		0		0
Parity Bit 2		1	0			0	1			0	0
Parity Bit 4				1	0	0	1				
Parity Bit 8								0	0	0	0
XOR Paritys	1	1		0				0			
Corrected Msg	0	0	1	1	0	0	1	0	0	0	0

Binary # when XOR the parity is the bit position with the error (e.g. 0011 = bit 3 is wrong)

Error Detection

- Less bits are required
 - if errors are infrequent, then then this works better
 - assumes that re-transmission is possible
- Cyclic Redundancy Codes (CRC)
 - Use a generator function G(x) of degree r
 - r+1 bits long
 - $x^5 + x^2 + 1$ is degree 5 and represented as 100101
 - let M' be the message with r 0's on the end of it
 - divide M' into G(x) and compute remainder
 - use this as the r bit CRC code
 - a code with r bits will detect all burst errors less than r bits

CRC's

several G's are standardized

$$- CRC-12 = x^{12} + x^{11} + x^3 + x^2 + x + 1$$

$$- CRC-16 = x^{16} + x^{15} + x^2 + 1$$

$$- CRC-CCITT = x^{16} + x^{12} + x^5 + 1$$

16 bit CRC will catch

- all single and double bit errors
- all errors with an odd number of bits
- all burst errors of length less than 16

CRC Example

Frame : 1101011011

Generator: 10011

Message after appending 4 zero bits: 1 1 0 1 0 1 1 0 0 0 0

 $0\ 0\ 0\ 0\ 0$

0 1 0 1 1 0 0 0

1 0 1 1 0 1 0 1 0

0 1 0 1 0 0 0 0 0

1 0 1 0 0 1 0 0 1 1

0 1 1 1 0

Division is done using XOR

 $\frac{0\ 0\ 0\ 0}{1\ 1\ 1\ 0}$ Remainder

Transmitted frame: 1 1 0 1 0 1 1 0 1 1 1 1 1 0

PPP Protocol

- Link Protocol for Serial Lines
 - Supports multiple network protocols: IP, IPX, CLNP, ...
 - designed for dialup or leased lines
- Link Establishment (via LCP Link Control Protocol)
 - Negotiate Options
 - configure-request: list of proposed options and values
 - configure-{ack/nack}: will (won't) use the requested option
 - Allows for authentication

flag Address control protocol payload checksum					
	flag 01111110	payload	protocol		

From: Computer Networks, 3rd Ed. by Andrew S. Tanenbaum, (c)1996 Prentice Hall.

PPP Cont.

- NCP protocol
 - per network level protocol
 - used to establish network attributes (e.g. addresses)
 - high bit of protocol # is a one
- Notes on Link Format
 - character stuff flag byte in data
 - Escape Character is 0x7d (0111 1101)
 - Escape Character and Frame Marker sent at
 - <Esc-Char><data XOR 0x20>
 - option to skip address and control fields (since constant)
- IP
 - Protocol byte (0x21) or 0x8021 for IP NCP