



Designing Parallel Programs

Abhinav Bhatele, Alan Sussman

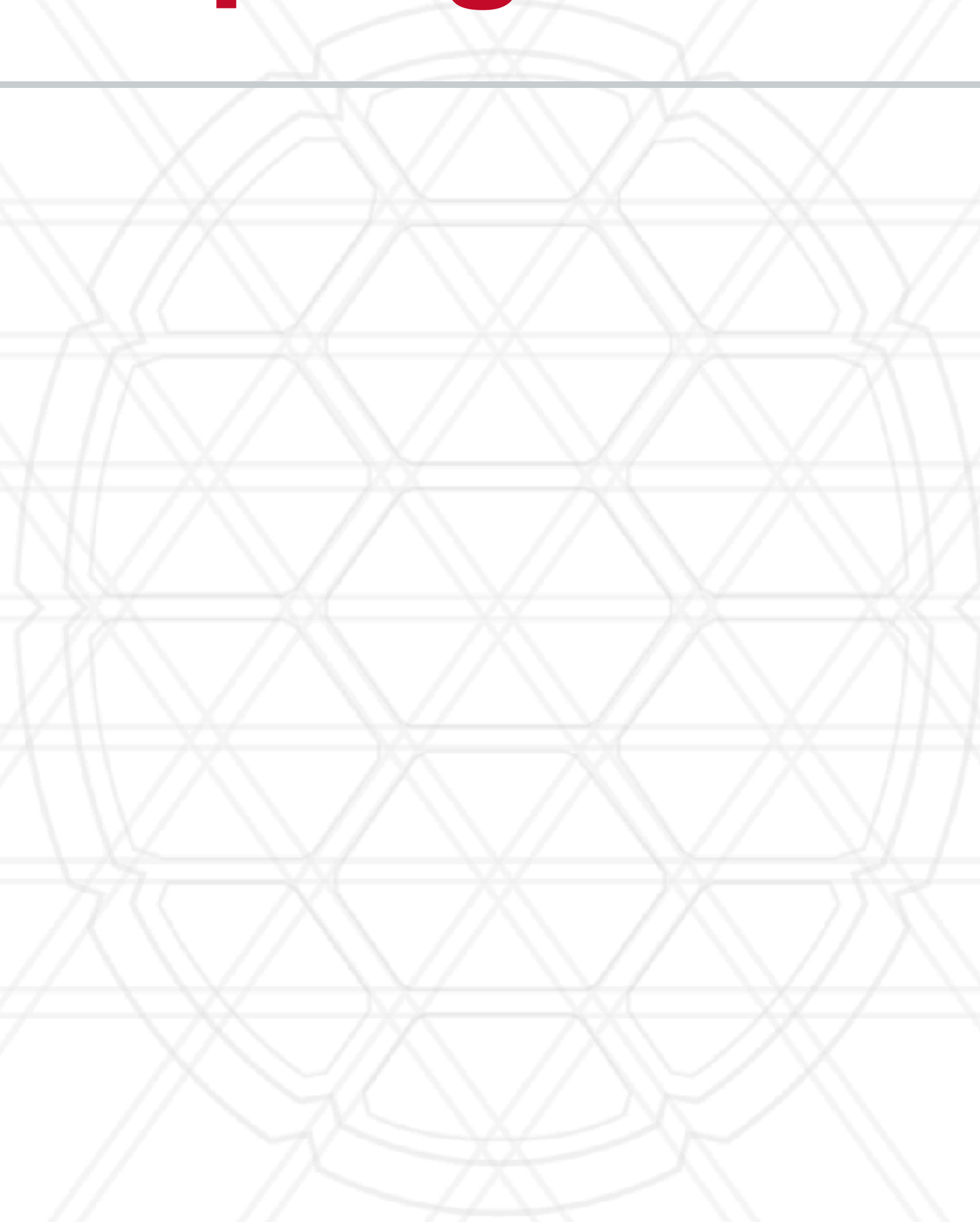


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Reminders / Announcements

- If you do not have a zaratan account, email: cm416@cs.umd.edu
- When emailing, please mention your course and section number:
 - Example: 416 / Section 0201
- Accomodations: please get the letters to the respective instructors soon
- Join piazza: <https://piazza.com/umd/fall2024/cm416cm616>
- Assignment 0 will be posted tonight Sep 3 11:59 pm, due on Sep 10 11:59 pm
- Office hours have been posted on the website

Writing parallel programs



Writing parallel programs

- Decide the serial algorithm first

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SPMD model

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 - Data locality: assignment of data to specific processes to minimize data movement

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- Computation: how to divide work among threads/processes?

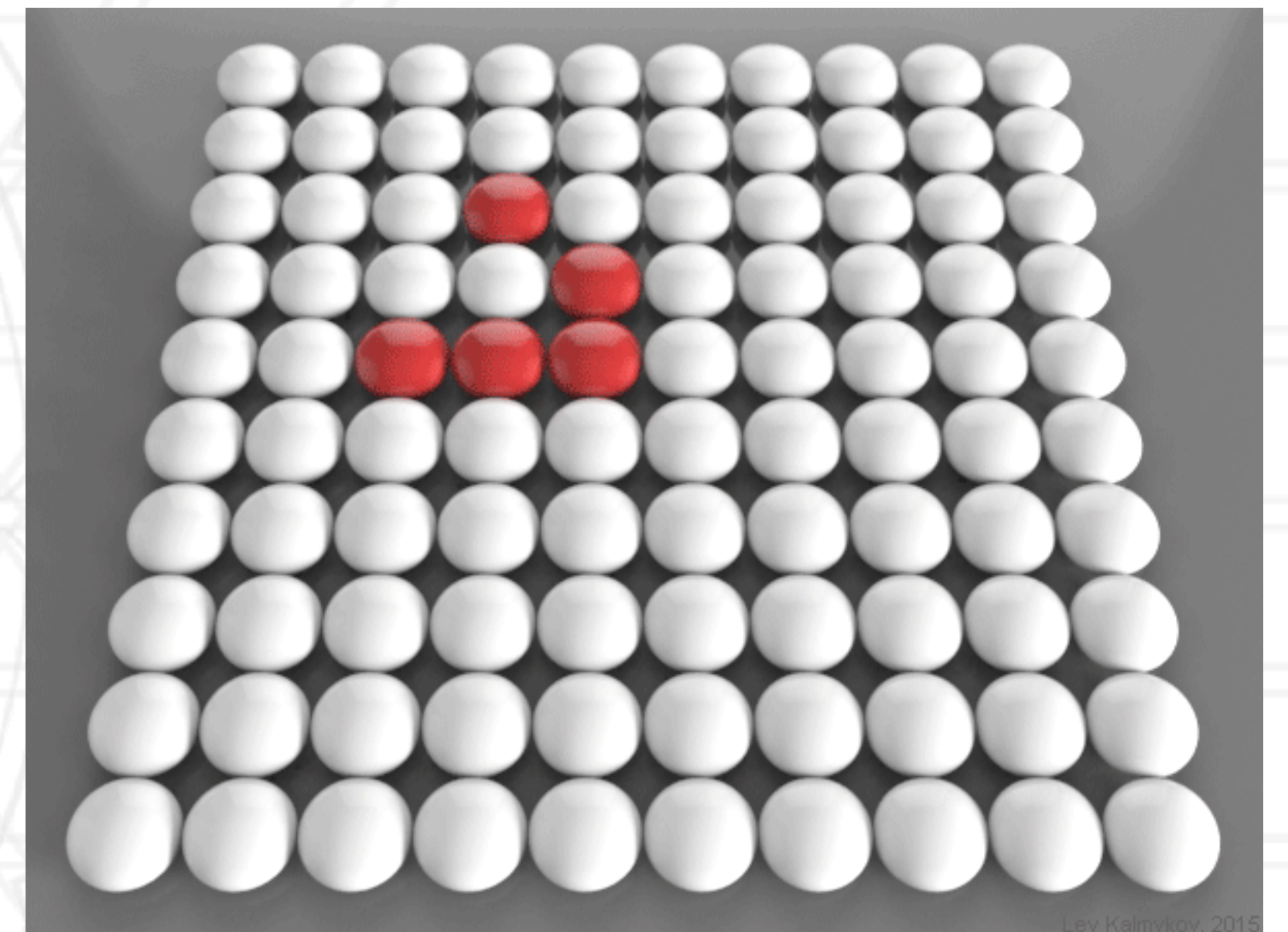
Writing parallel programs

SPMD model

- Decide the serial algorithm first
- Data: how to distribute data among threads/processes?
 - Data locality: assignment of data to specific processes to minimize data movement
- Computation: how to divide work among threads/processes?
- Figure out how often communication will be needed

Conway's Game of Life

- Two-dimensional grid of (square) cells
- Each cell can be in one of two states: live or dead
- Every cell only interacts with its eight nearest neighbors
- In every generation (or iteration or time step), there are some rules that decide if a cell will continue to live or die or be born (dead → live)

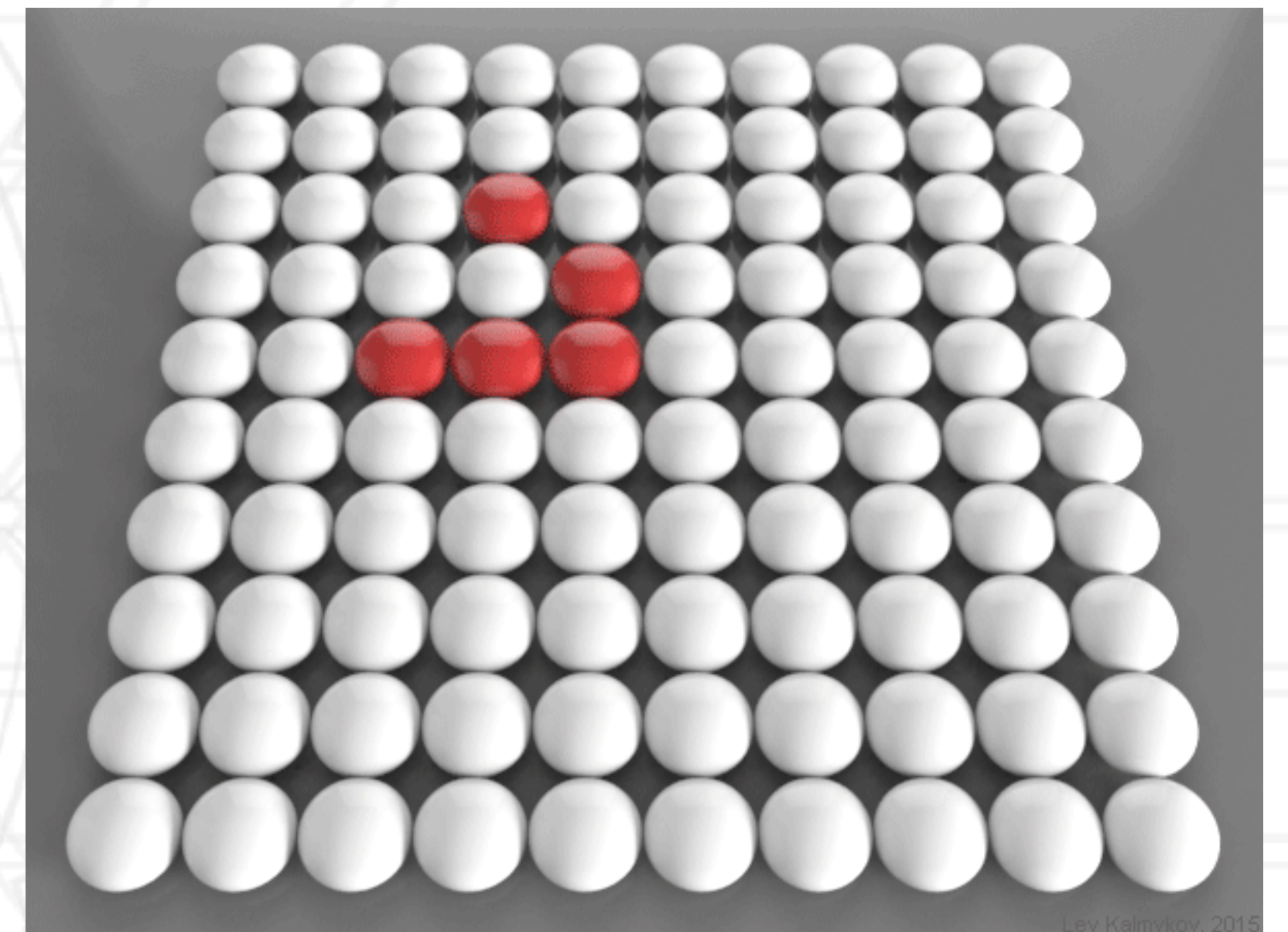


https://en.wikipedia.org/wiki/Conway's_Game_of_Life

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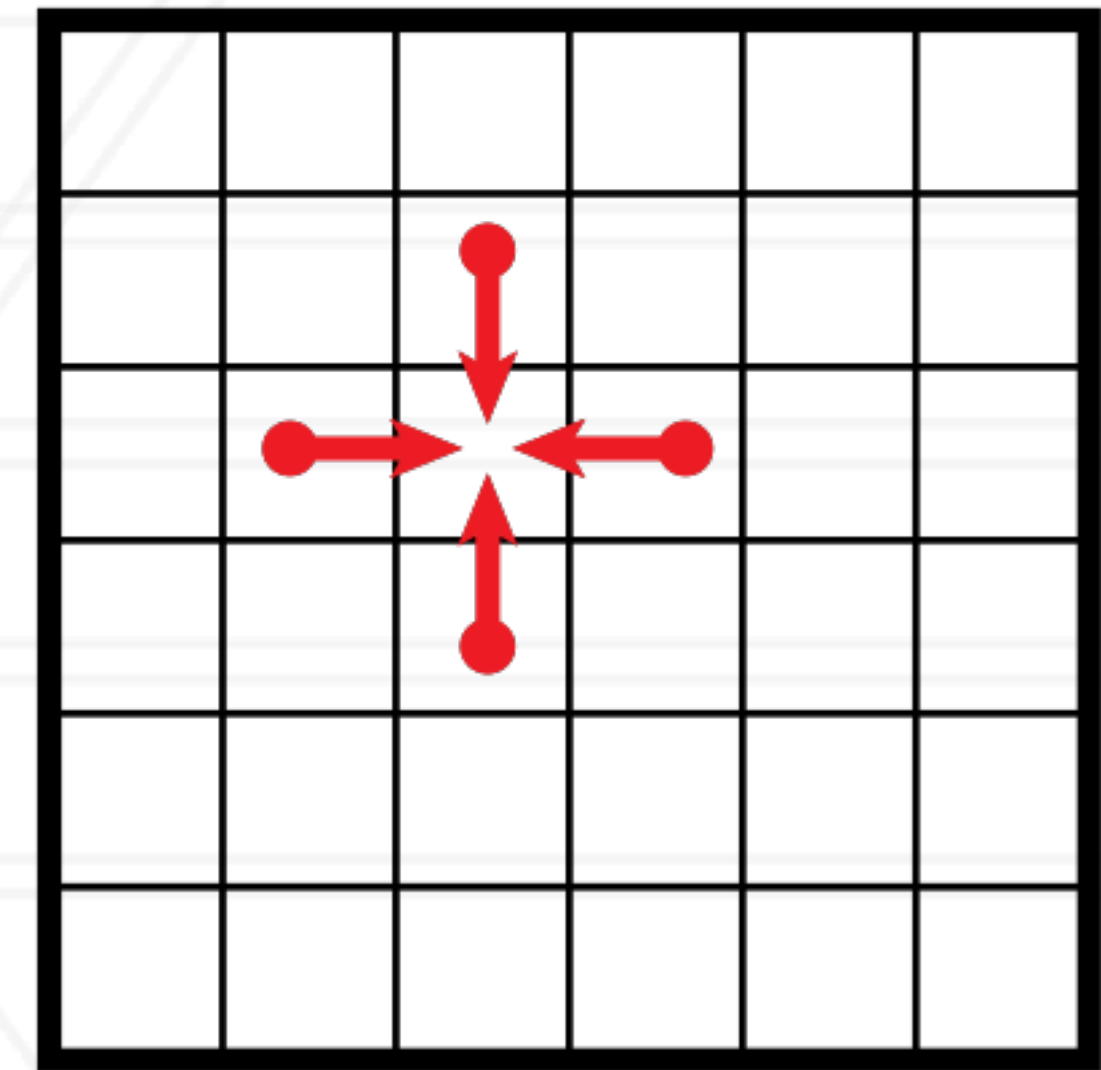
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Two-dimensional stencil computation

- Commonly found kernel in computational codes
- Heat diffusion, Jacobi method, Gauss-Seidel method

2D 5-point Stencil

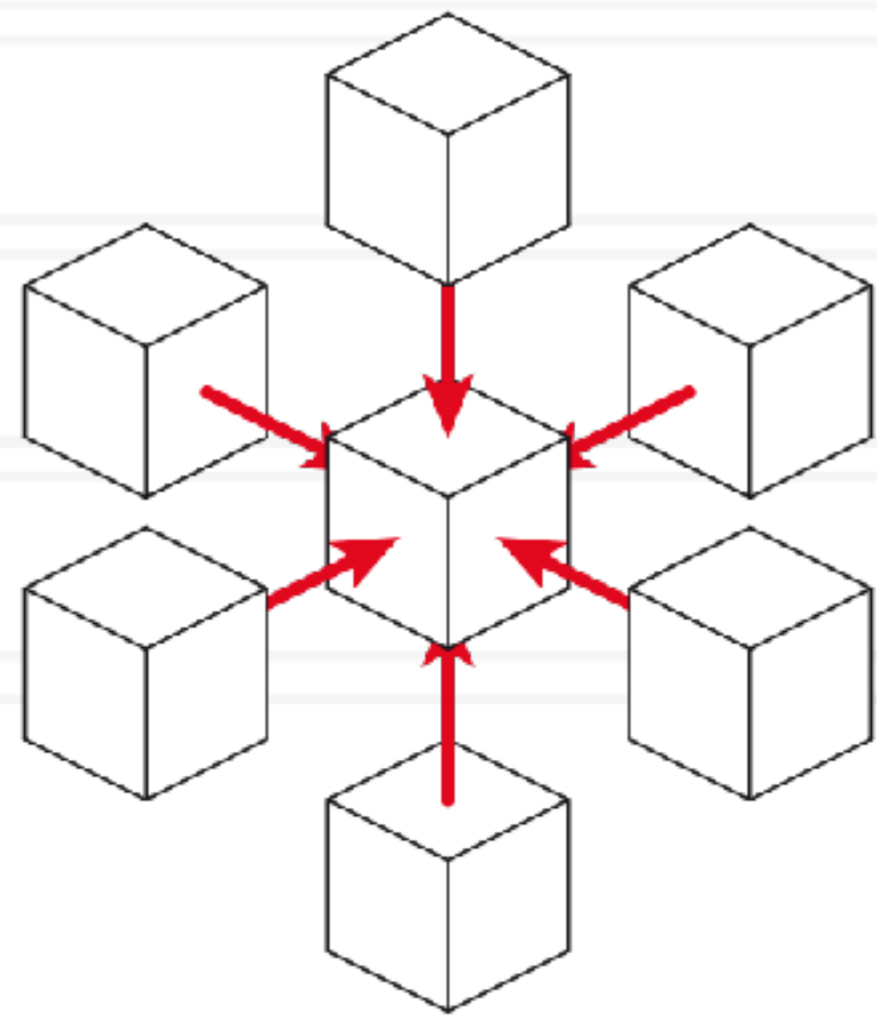
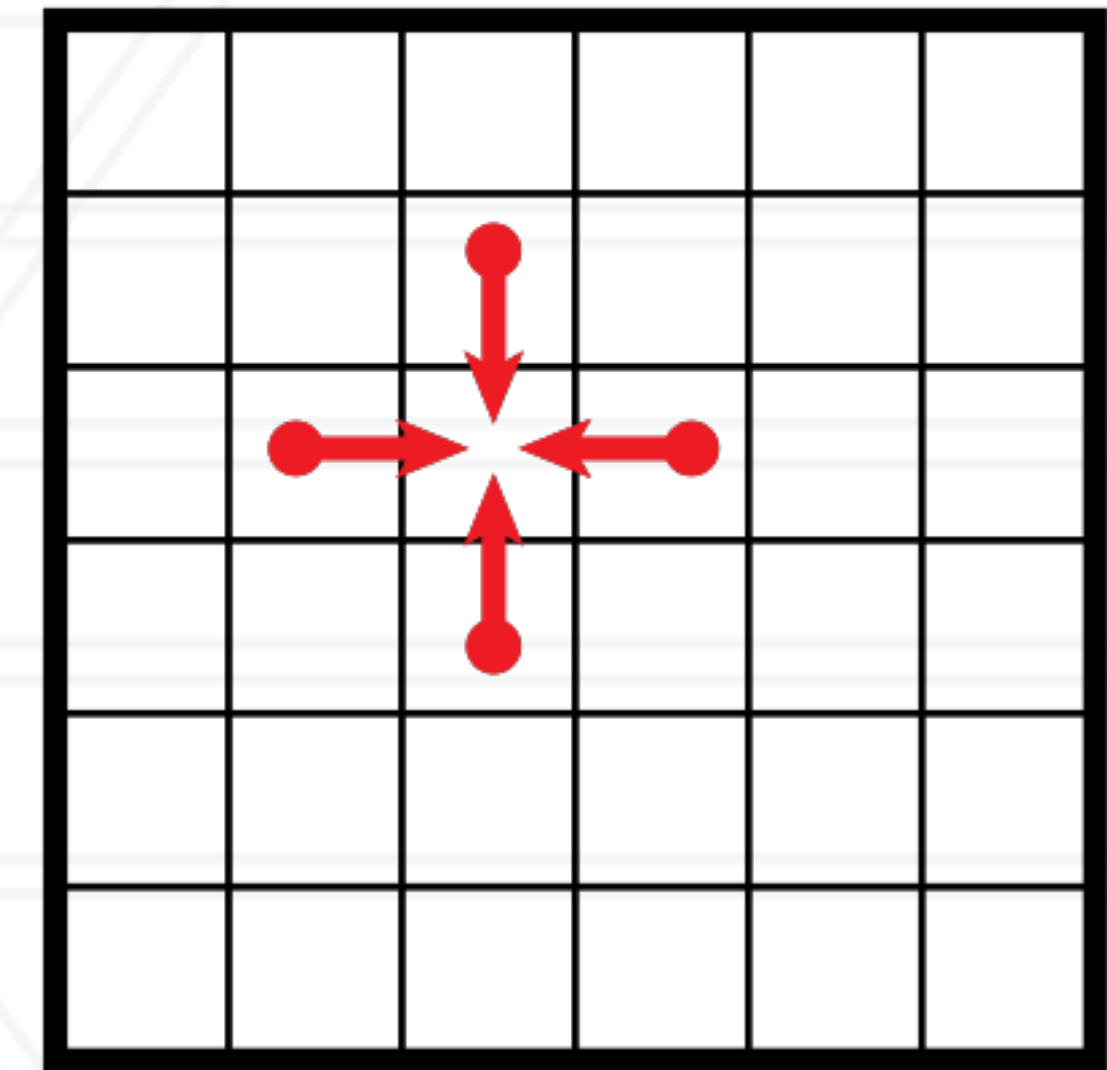


$$A[i, j] = \frac{A[i, j] + A[i - 1, j] + A[i + 1, j] + A[i, j - 1] + A[i, j + 1]}{5}$$

Two-dimensional stencil computation

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2D 5-point Stencil



3D 7-point Stencil

$$A[i, j] = \frac{A[i, j] + A[i - 1, j] + A[i + 1, j] + A[i, j - 1] + A[i, j + 1]}{5}$$

Serial code

```
for(int t=0; t<num_steps; t++) {  
    ...  
  
    for(i ...)  
        for(j ...)  
            A_new[i, j] = (A[i, j] + A[i-1, j] + A[i+1, j] + A[i, j-1] + A[i, j+1]) * 0.2  
  
    // copy contents of A_new into A  
    ...  
}
```

Serial code

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for(int t=0; t<num_steps; t++) {  
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```

Why do we keep two copies of A?

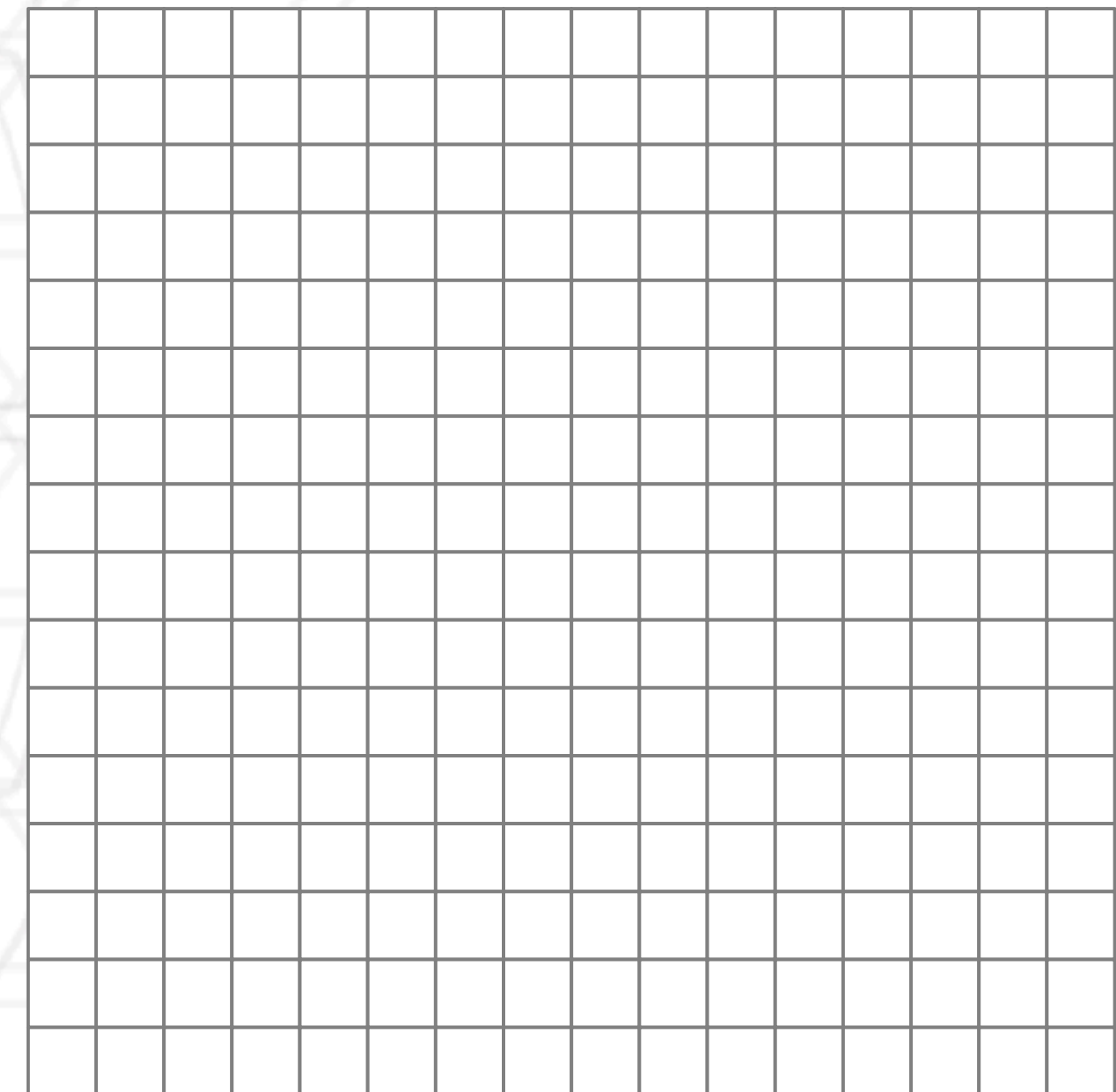
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    ...  
}
```

Why do we keep two copies of A?

For correctness, we have to ensure that elements in A are not written into before they are read in the same timestep / iteration

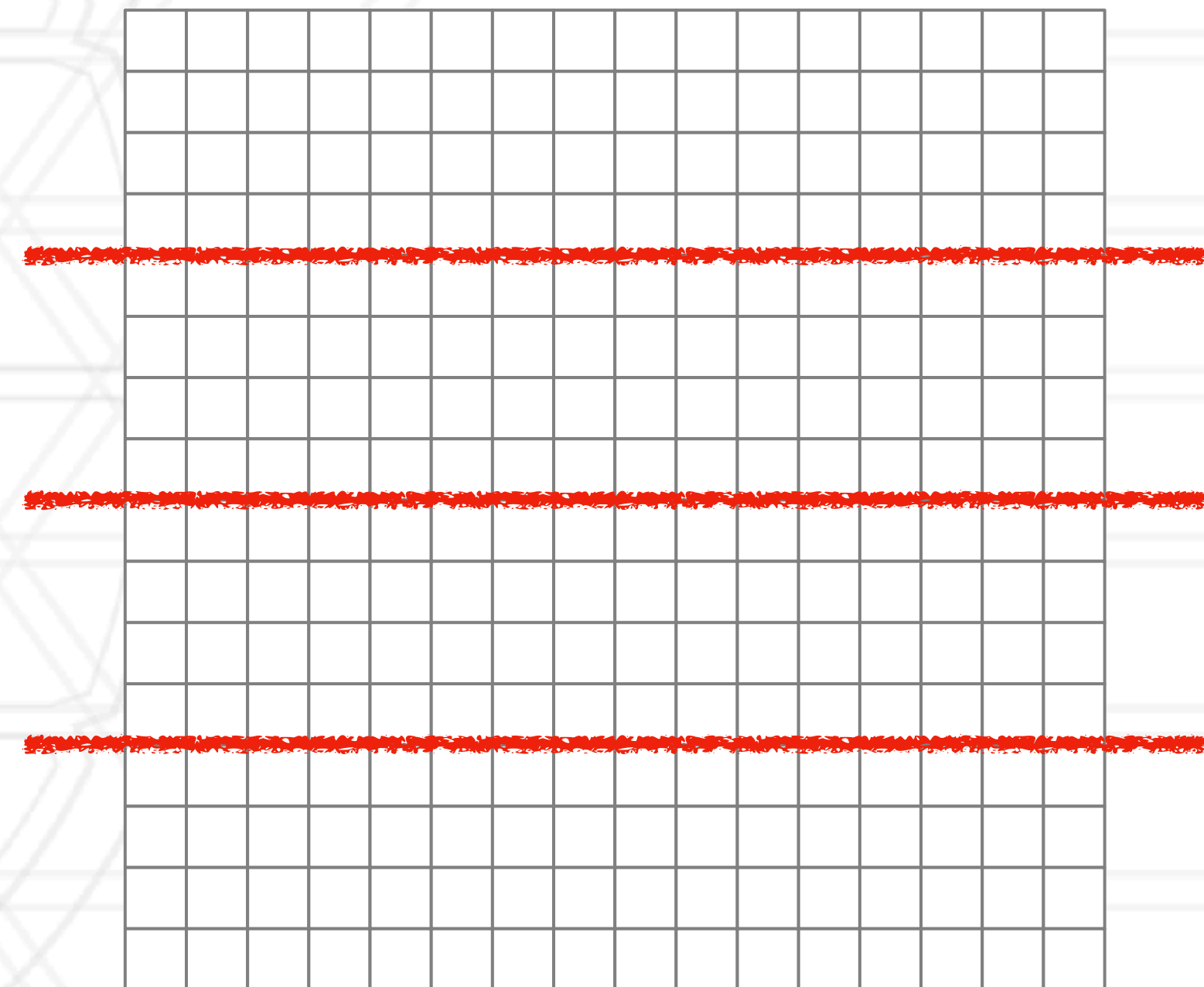
2D stencil computation in parallel



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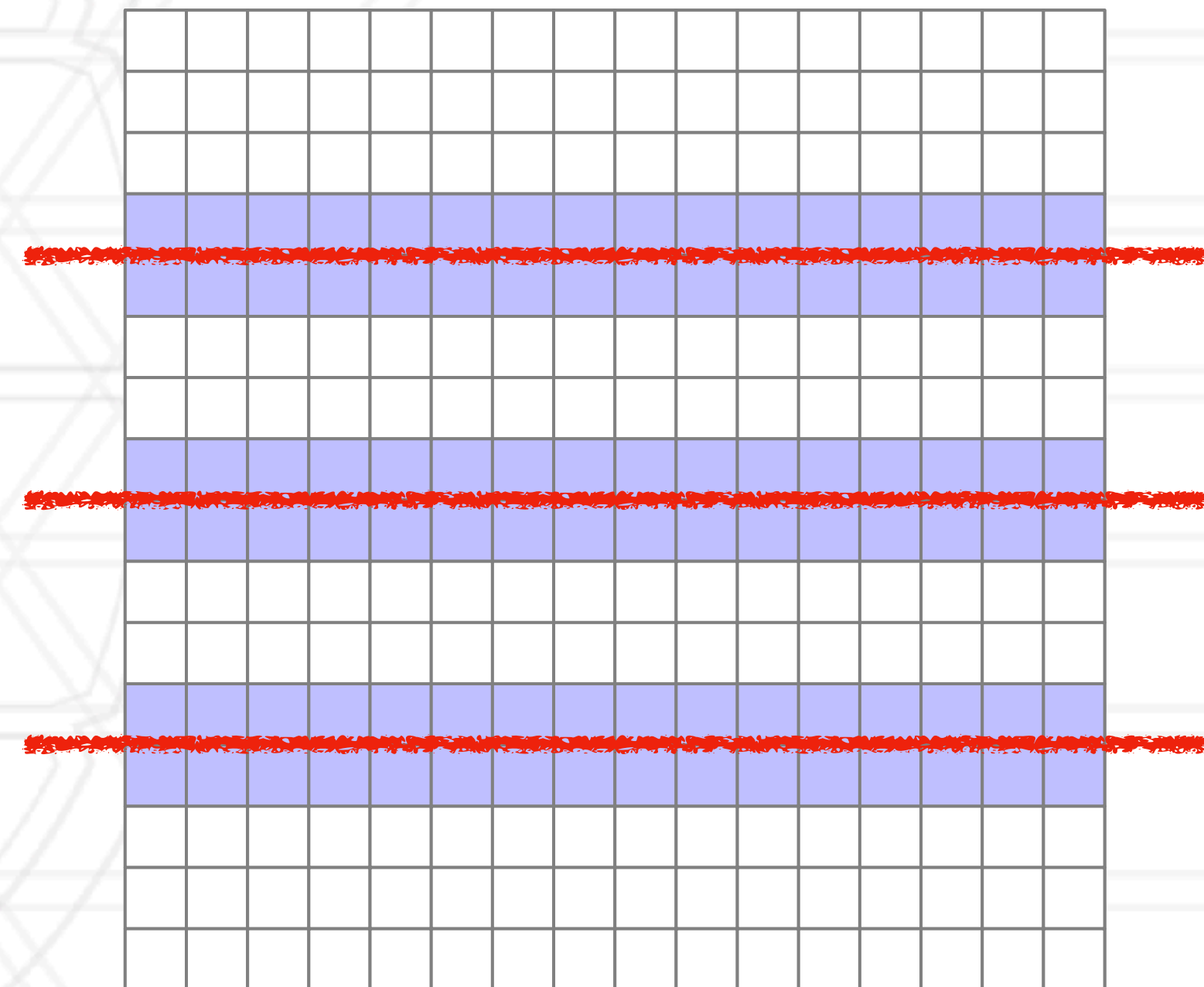
- 1D decomposition

- Divide rows (or columns) among processes
- Each process has to communicate with two neighbors (above and below)



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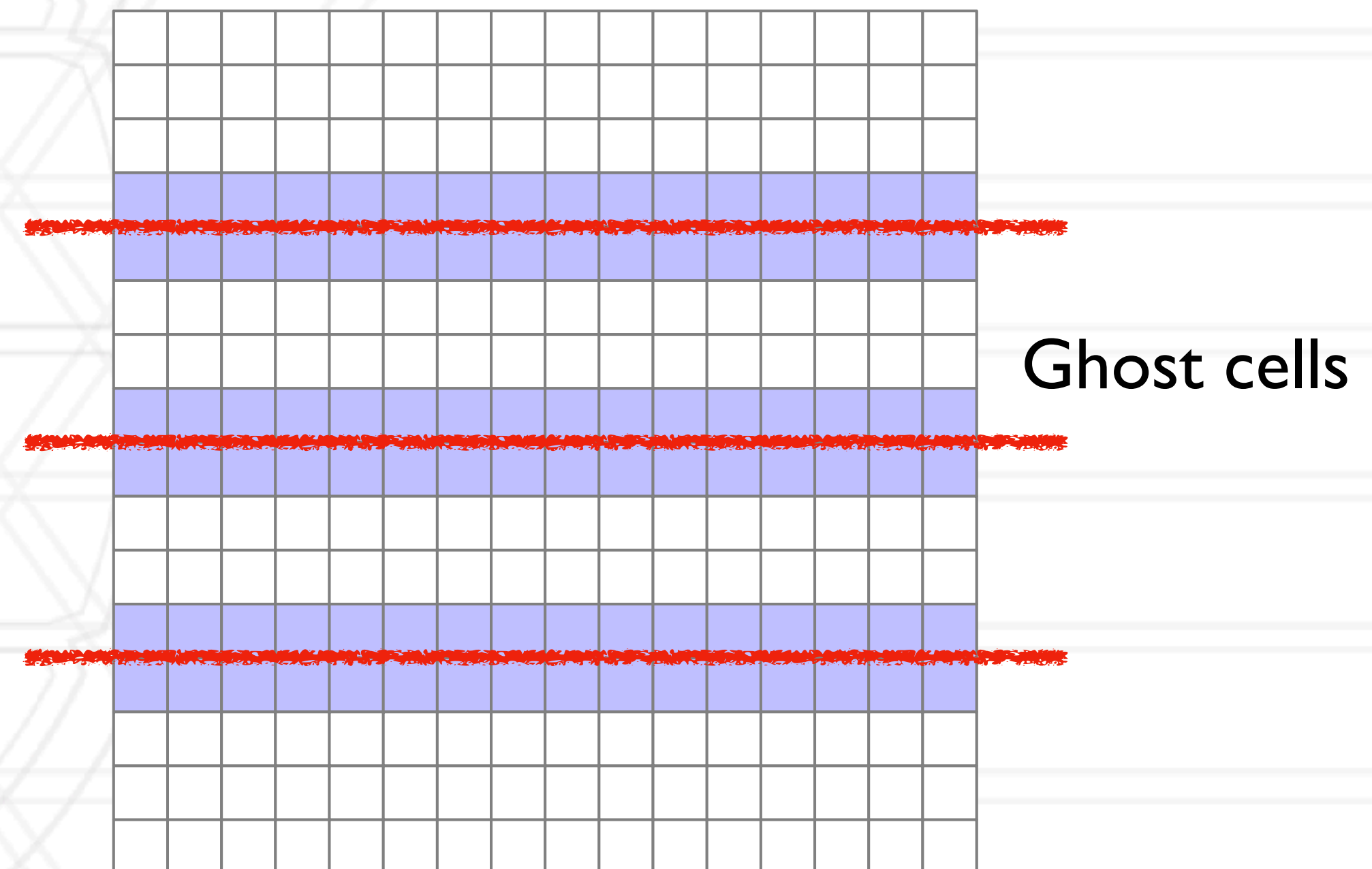
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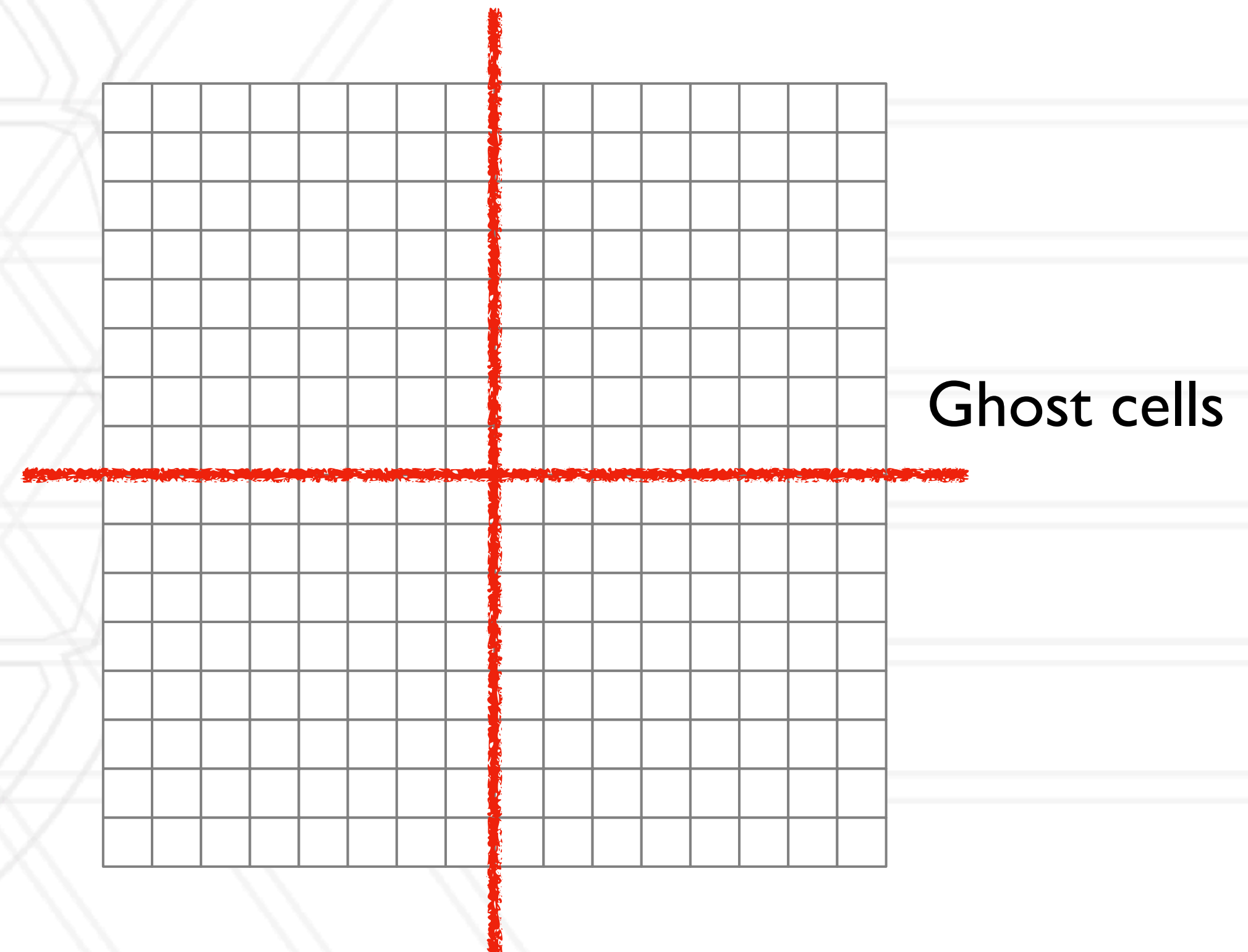
2D stencil computation in parallel

- 1D decomposition

- Divide rows (or columns) among processes
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- 2D decomposition

- Divide both rows and columns (2d blocks) among processes
- Each process has to communicate with four neighbors



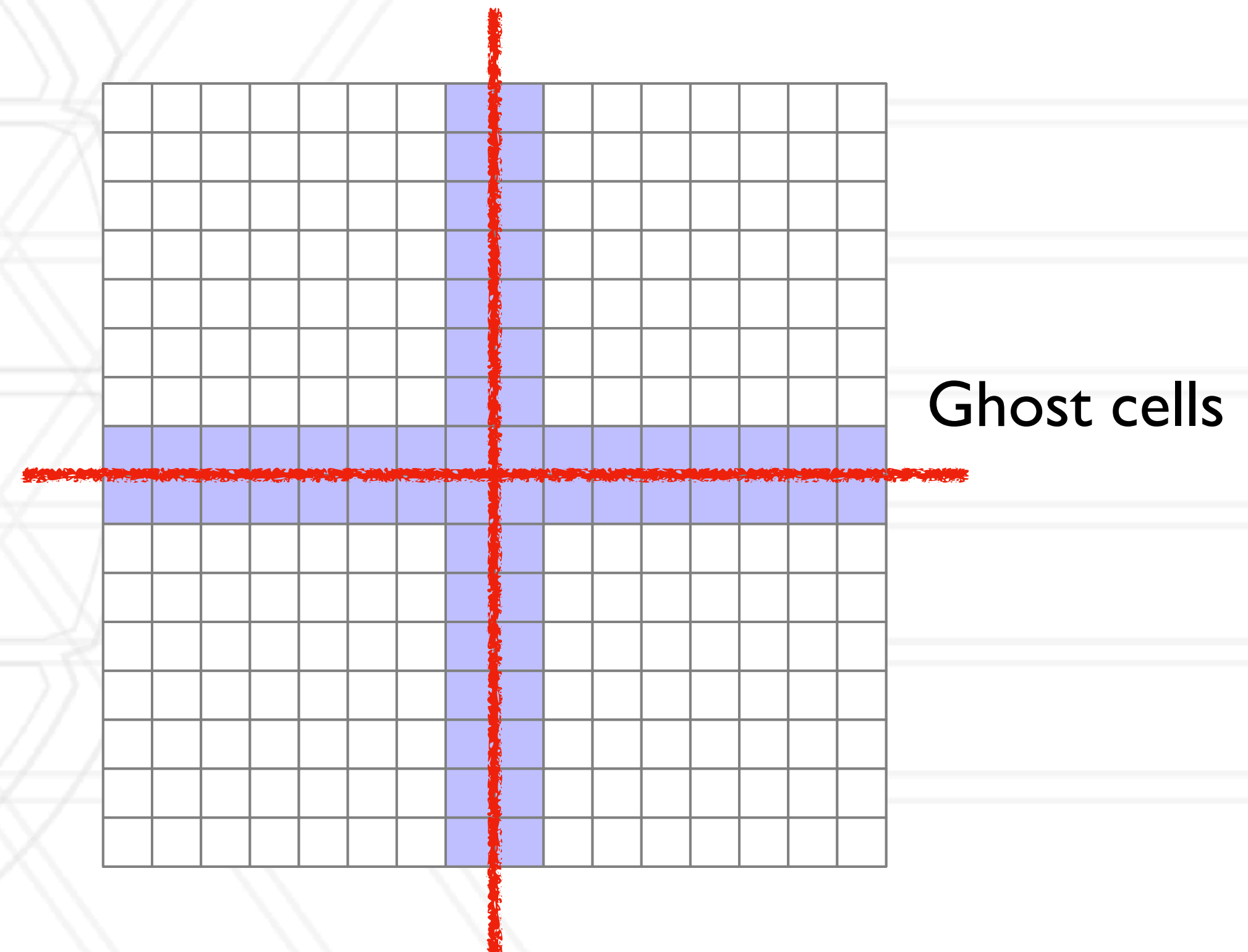
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Prefix sum

- Calculate sums of prefixes (running totals) of elements (numbers) in an array
- Also called a “scan” sometimes

```
pSum[0] = A[0]
```

```
for(i=1; i<N; i++) {  
    pSum[i] = pSum[i-1] + A[i]  
}
```

A	1	2	3	4	5	6	...
pSum	1	3	6	10	15	21	...

Parallel prefix sum

2	8	3	5	7	4	1	6
---	---	---	---	---	---	---	---

Parallel prefix sum

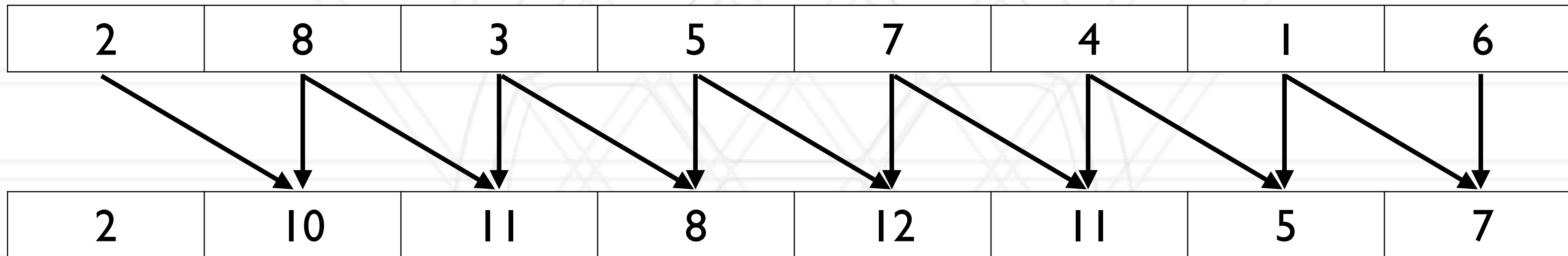
Processes/
threads

0	1	2	3	4	5	6	7
2	8	3	5	7	4	1	6

Parallel prefix sum

Processes/
threads

0 1 2 3 4 5 6 7



Stride 1

Parallel prefix sum

Processes/
threads

0 1 2 3 4 5 6 7

2	8	3	5	7	4	1	6
---	---	---	---	---	---	---	---

Stride 1

2	10	11	8	12	11	5	7
---	----	----	---	----	----	---	---

Stride 2

2	10	13	18	23	19	17	18
---	----	----	----	----	----	----	----

Parallel prefix sum

Processes/
threads

0 1 2 3 4 5 6 7

2	8	3	5	7	4	1	6
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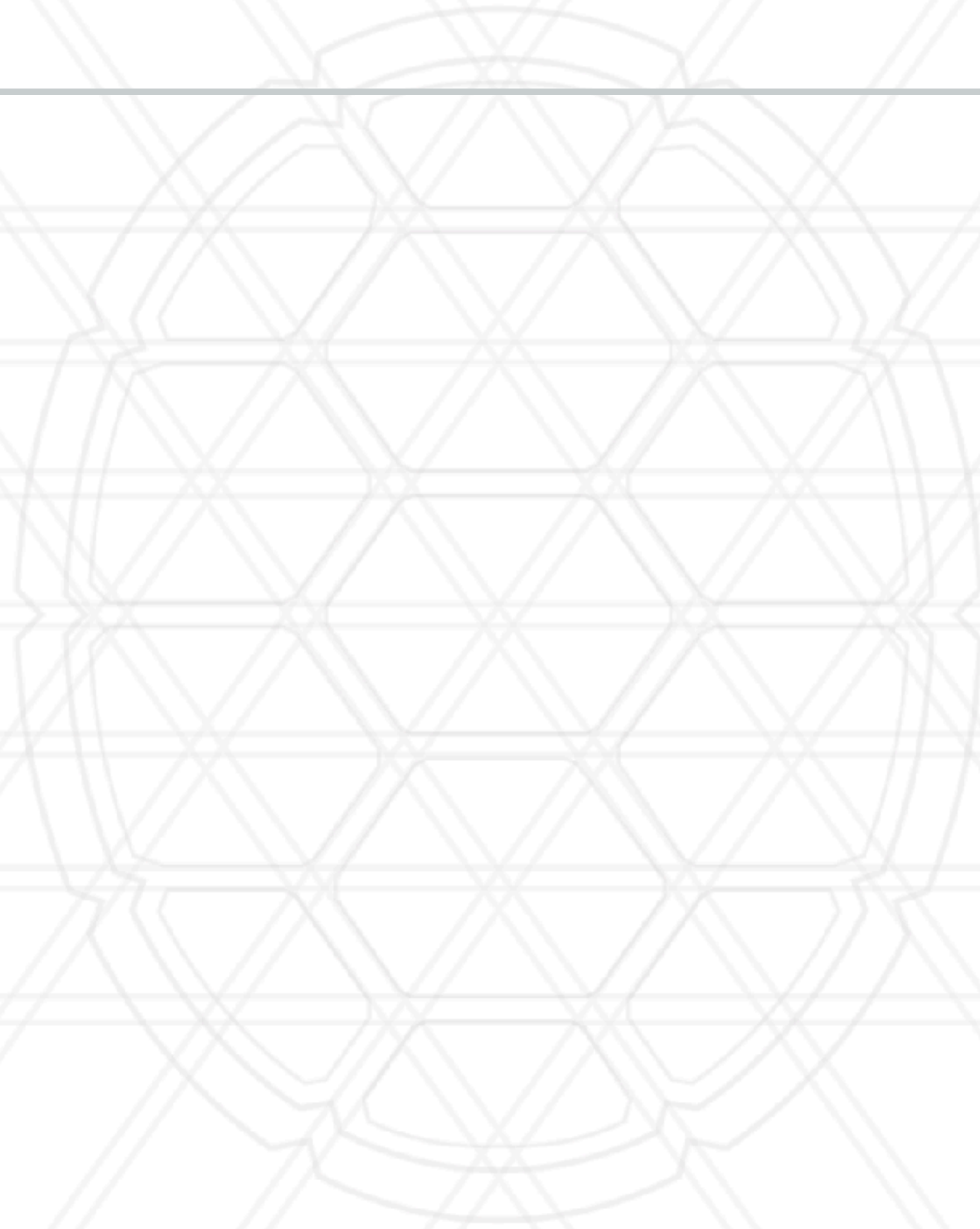
Stride 2

2	10	13	18	23	19	17	18
---	----	----	----	----	----	----	----

Stride 4

2	10	13	18	25	29	30	36
---	----	----	----	----	----	----	----

In practice



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 - Do the serial prefix sum calculation for the blocks owned on each process locally

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- You have N numbers and p processes, $N \gg p$
- Assign a N/p block to each process
 - Do the serial prefix sum calculation for the blocks owned on each process locally
- Then do parallel algorithm with partial prefix sums (using the last element from each local block)
 - Last element from sending process is added to all elements in receiving process' sub-block

Load balance and grain size

- **Load balance:** try to balance the amount of work (computation) assigned to different threads/ processes
 - Bring ratio of maximum to average load as close to 1.0 as possible
 - Secondary consideration: also load balance amount of communication
- **Grain size:** ratio of computation-to-communication
 - Coarse-grained (more computation) vs. fine-grained (more communication)



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