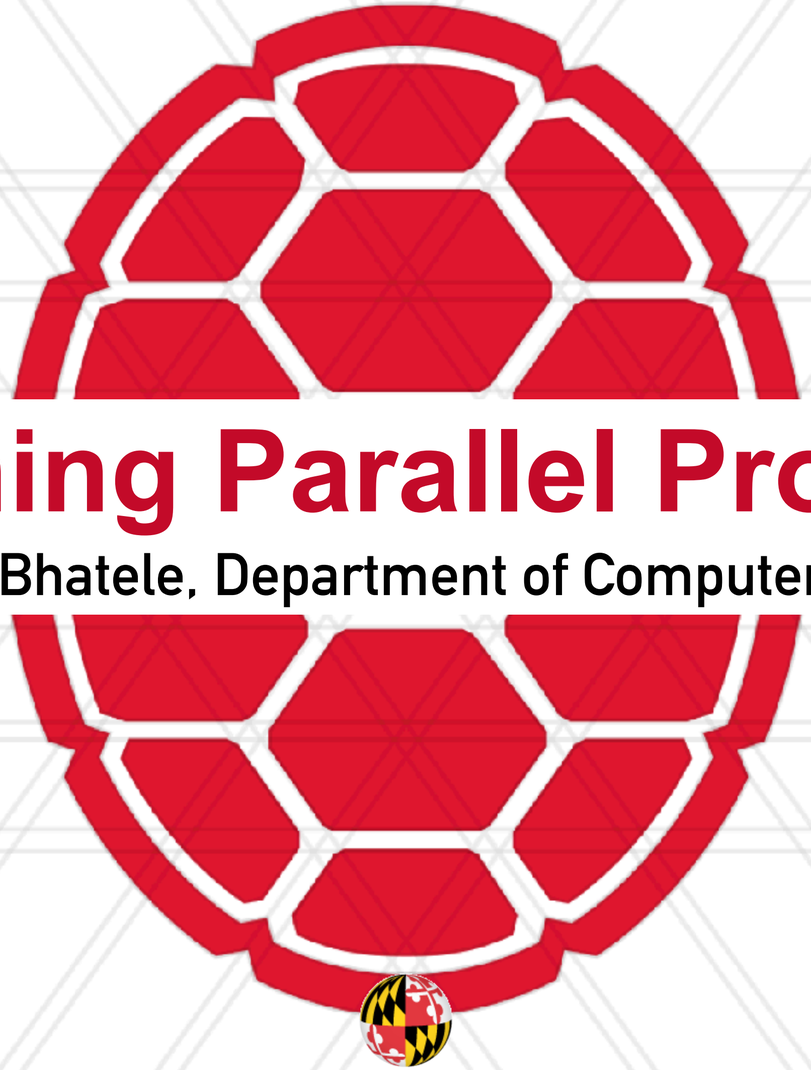
Introduction to Parallel Computing (CMSC416 / CMSC616)



Designing Parallel Programs

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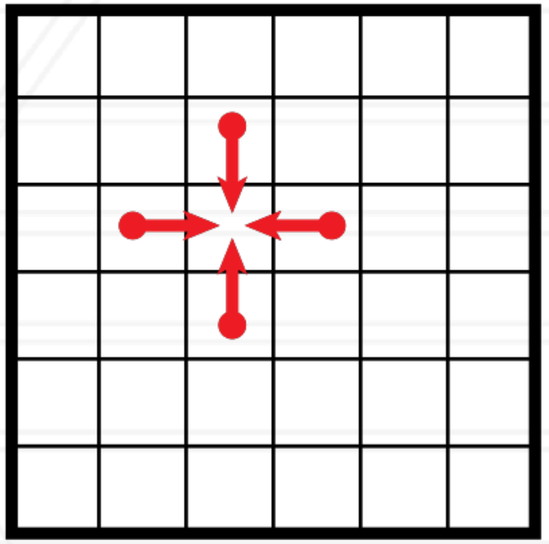
Writing parallel programs

- Decide the serial algorithm first
- Data: how to distribute data among threads/processes?
  - Data locality: assignment of data to specific processes to minimize data movement
- Computation: how to divide work among threads/processes?
- Figure out how often communication will be needed

Two-dimensional stencil computation

- Commonly found kernel in computational codes
- Heat diffusion, Jacobi method, Gauss-Seidel method



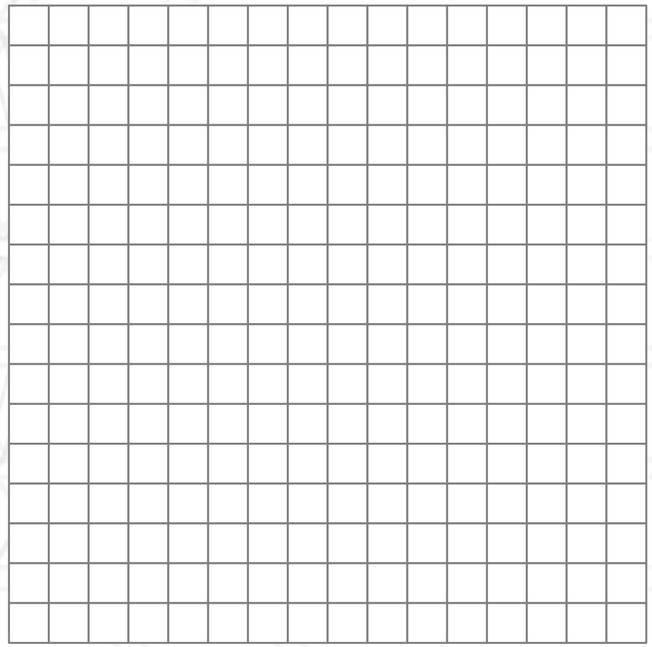
$$A[i,j] = \frac{A[i,j] + A[i-1,j] + A[i+1,j] + A[i,j-1] + A[i,j+1]}{5}$$

Serial code

Serial code

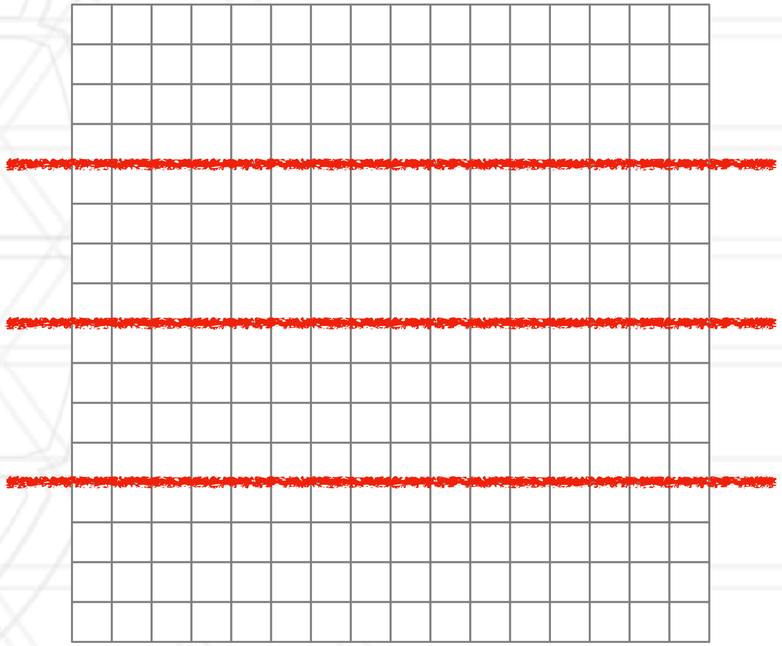
```
for(int t=0; t<num_steps; t++) {
  ...

  for(i ...)
    for(j ...)
      A_new[i, j] = (A[i, j] + A[i-1, j] + A[i+1, j] + A[i, j-1] + A[i, j+1]) * 0.2


  // copy contents of A_new into A
  ...
}
```

2D stencil computation in parallel



2D stencil computation in parallel

- 1D decomposition
  - Divide rows (or columns) among processes



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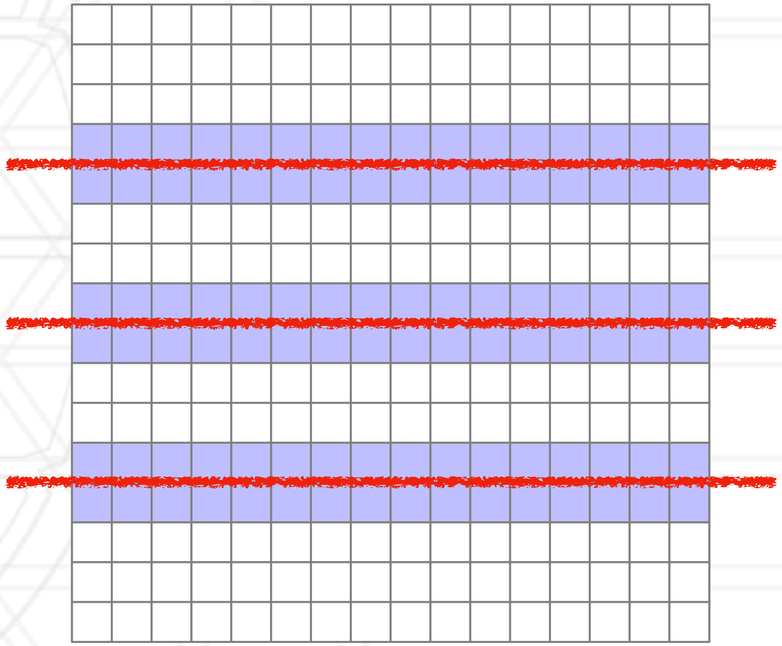
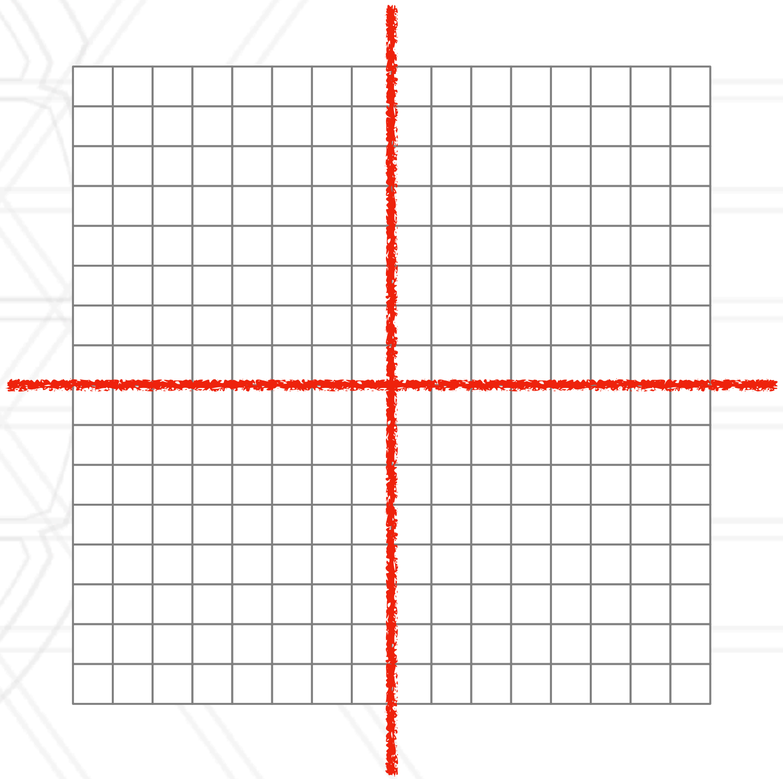


2D stencil computation in parallel

- 1D decomposition
  - Divide rows (or columns) among processes
- 2D decomposition
  - Divide both rows and columns (2d blocks) among processes



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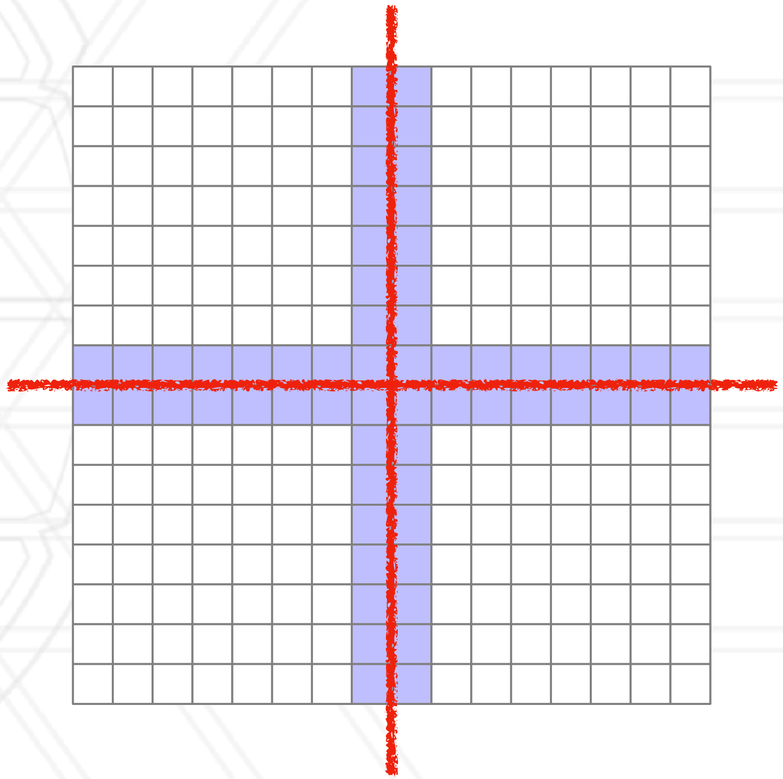


- 2D decomposition
  - Divide both rows and columns (2d blocks) among processes

Prefix sum

- Calculate partial sums of elements in array
- Also called a "scan" sometimes

```
pSum[0] = A[0]

for(i=1; i<N; i++) {
    pSum[i] = pSum[i-1] + A[i]
}
```

A	1	2	3	4	5	6	…
pSum	1	3	6	10	15	21	…

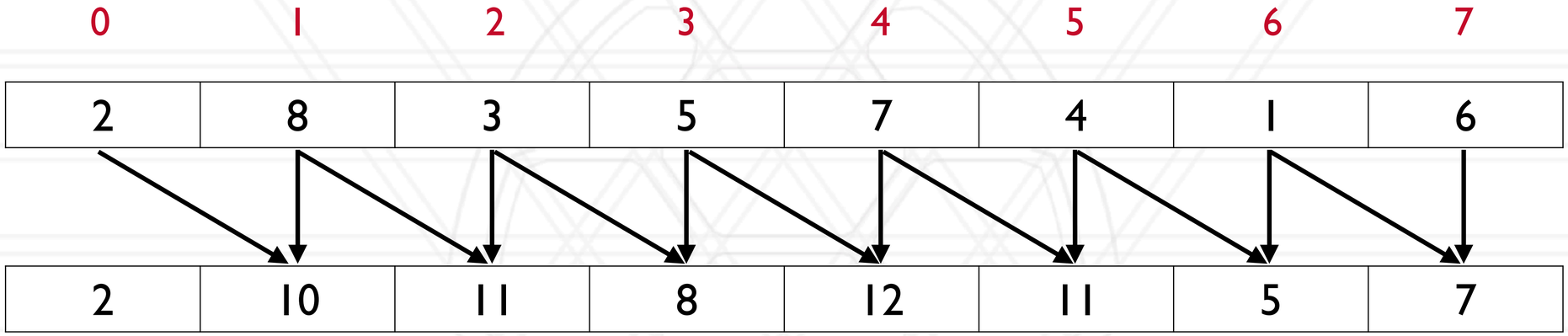
Parallel prefix sum

2	8	3	5	7	4	1	6

Parallel prefix sum

0	1	2	3	4	5	6	7
2	8	3	5	7	4	1	6

Parallel prefix sum



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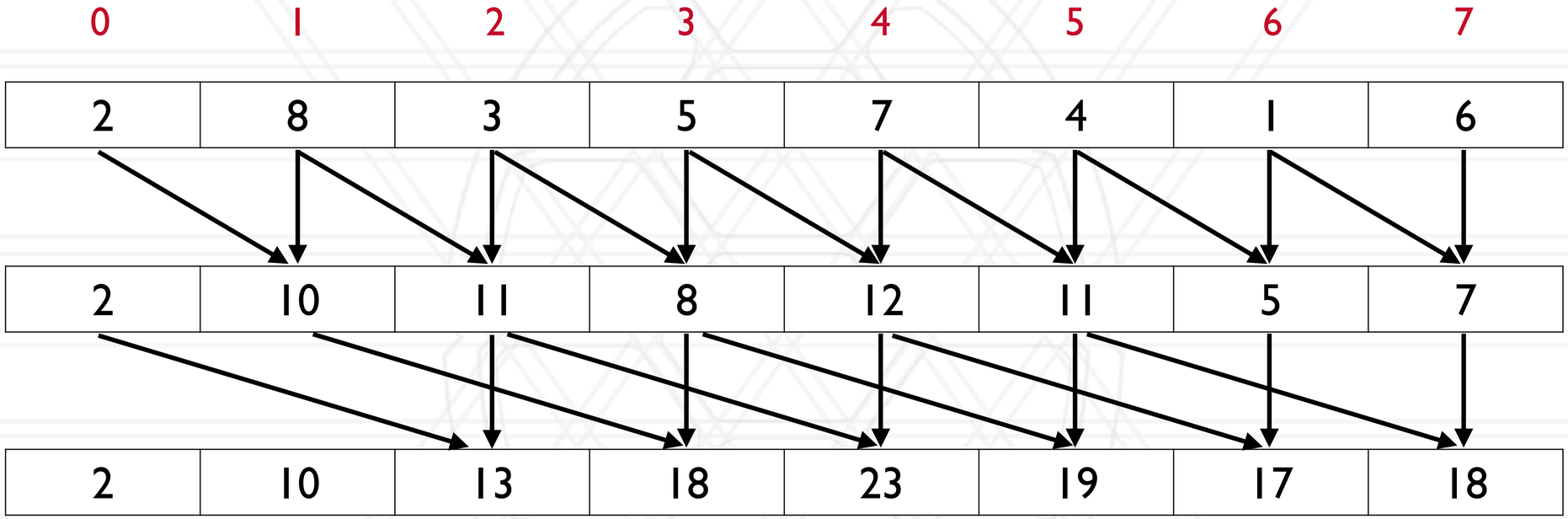

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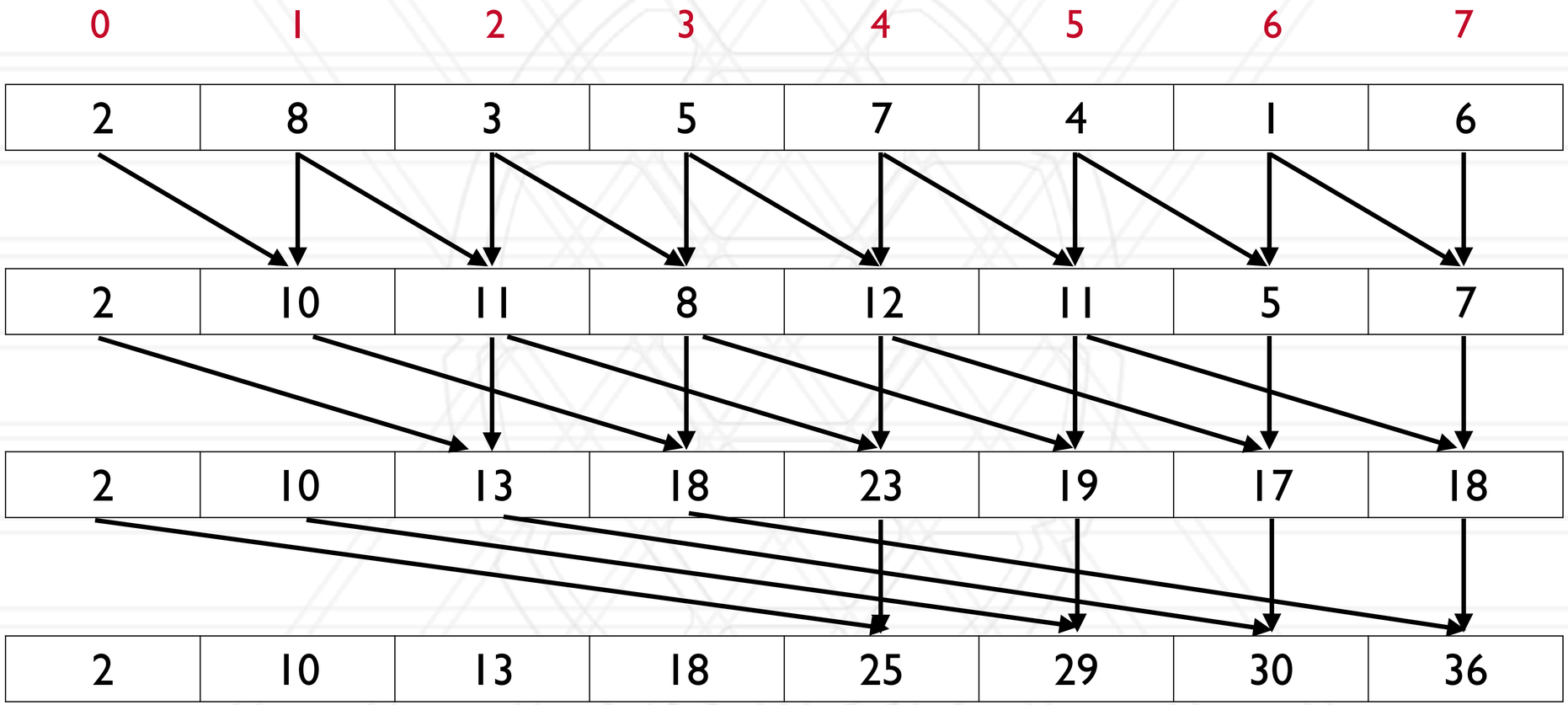

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  - Do calculation for the blocks on each process locally

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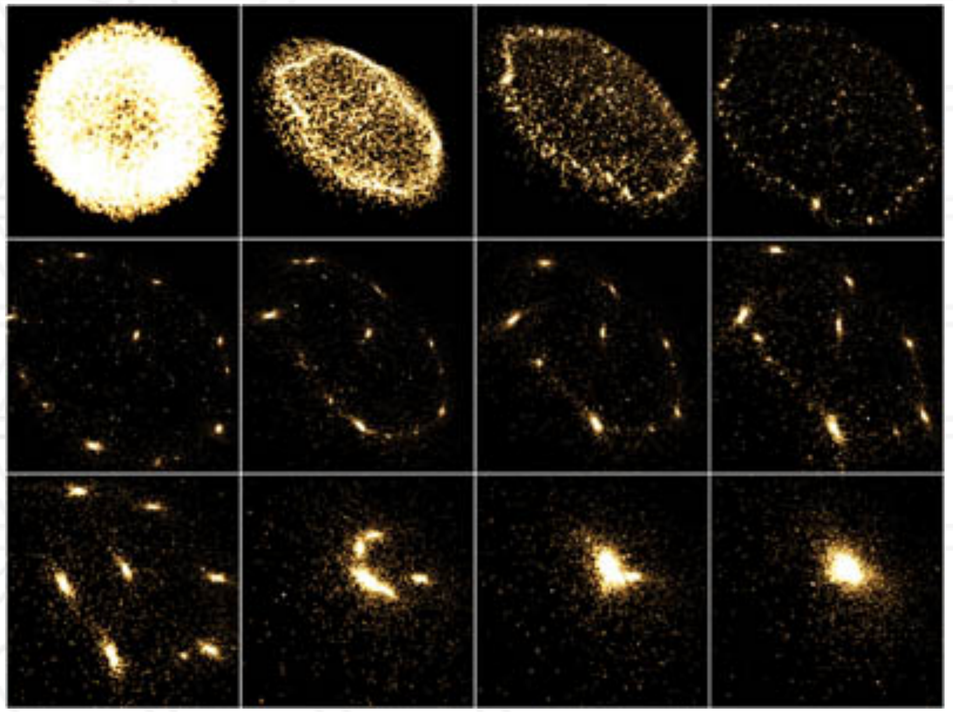
- You have N numbers and P processes, N >> P
- Assign a N/P block to each process
  - Do calculation for the blocks on each process locally
- Then do parallel algorithm with partial prefix sums

The *n*-body problem

- Simulate the motion of celestial objects interacting with one another due to gravitational forces
- Naive algorithm: $O(n^2)$
  - Every body calculates forces pair-wise with every other body (particle)



https://developer.nvidia.com/gpugems/gpugems3/part-v-physics-simulation/chapter-31-fast-n-body-simulation-cuda

Data distribution in *n*-body problems

- Naive approach: Assign n/p particles to each process
- Other approaches?

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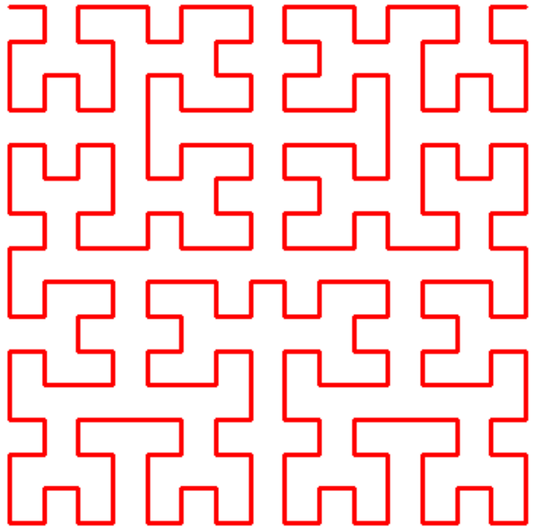
Space-filling curves



http://datagenetics.com/blog/march22013/

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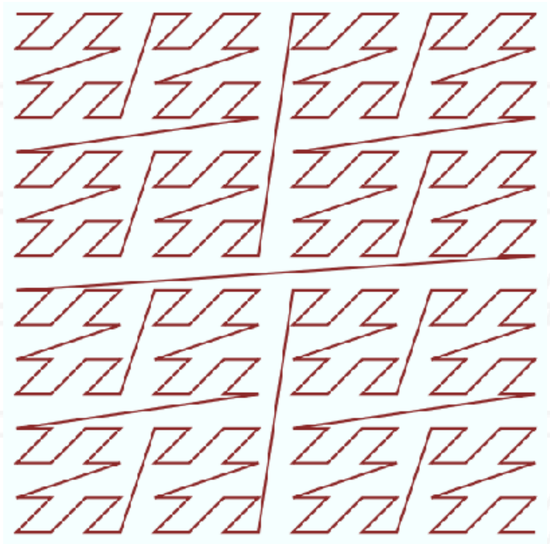

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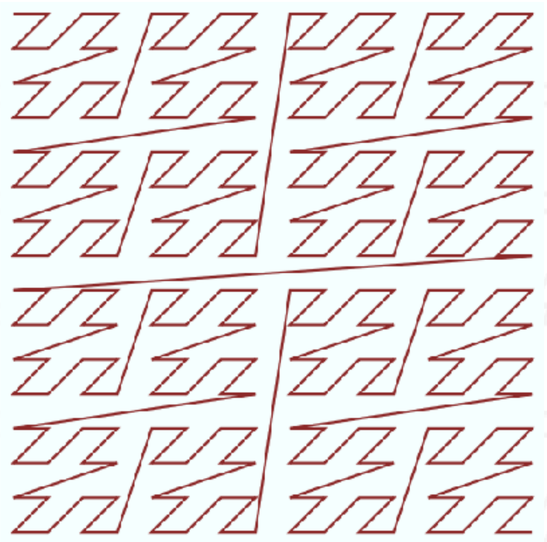

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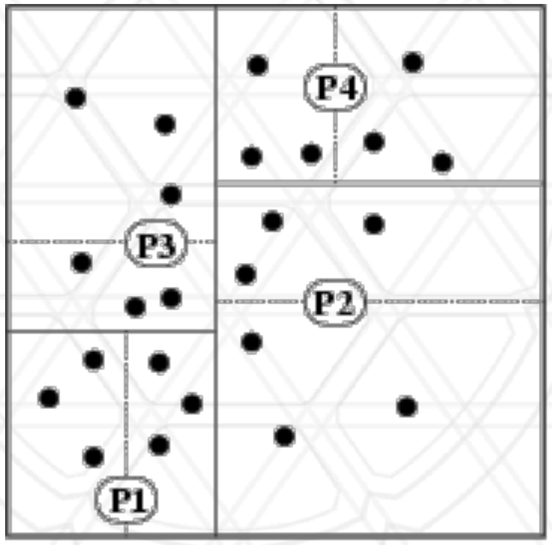
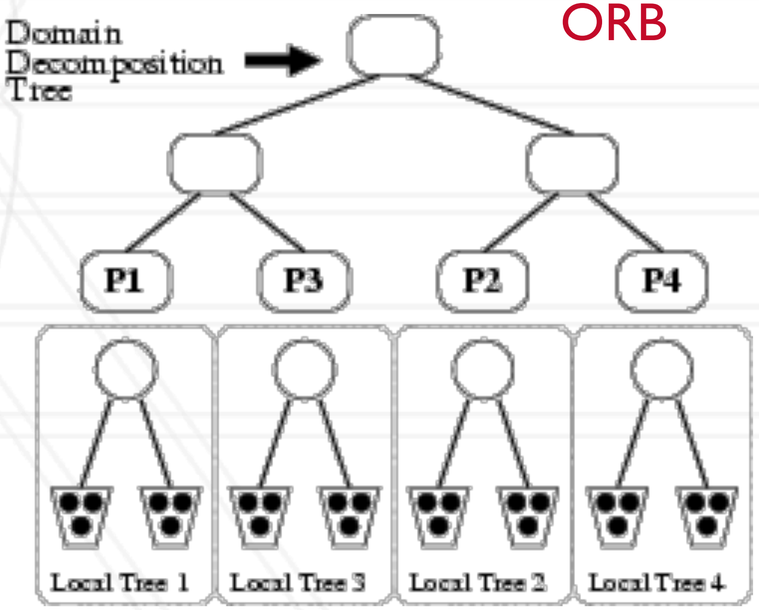


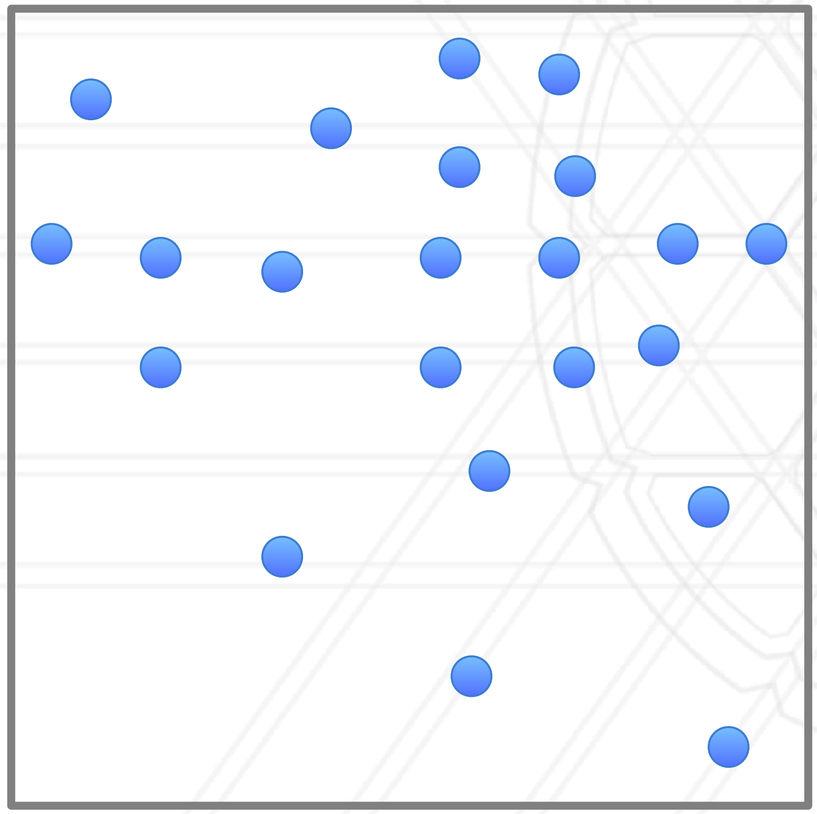
ORB



http://charm.cs.uiuc.edu/workshops/charmWorkshop2011/slides/CharmWorkshop2011_apps_ChaNGa.pdf

Data distribution in *n*-body problems

- Let us consider a two-dimensional space with bodies/particles in it



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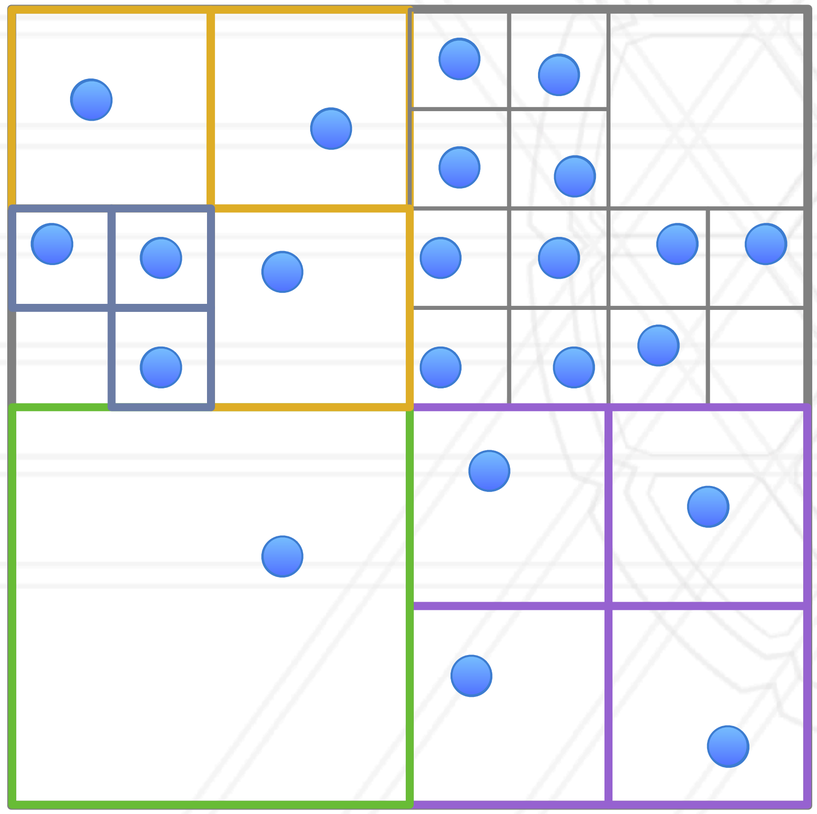

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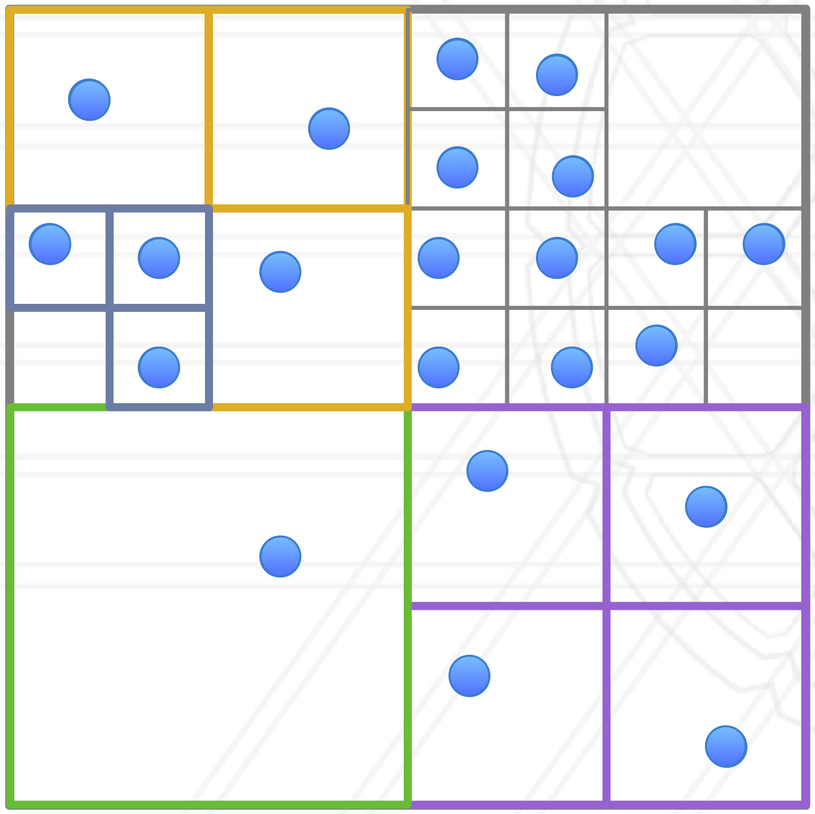

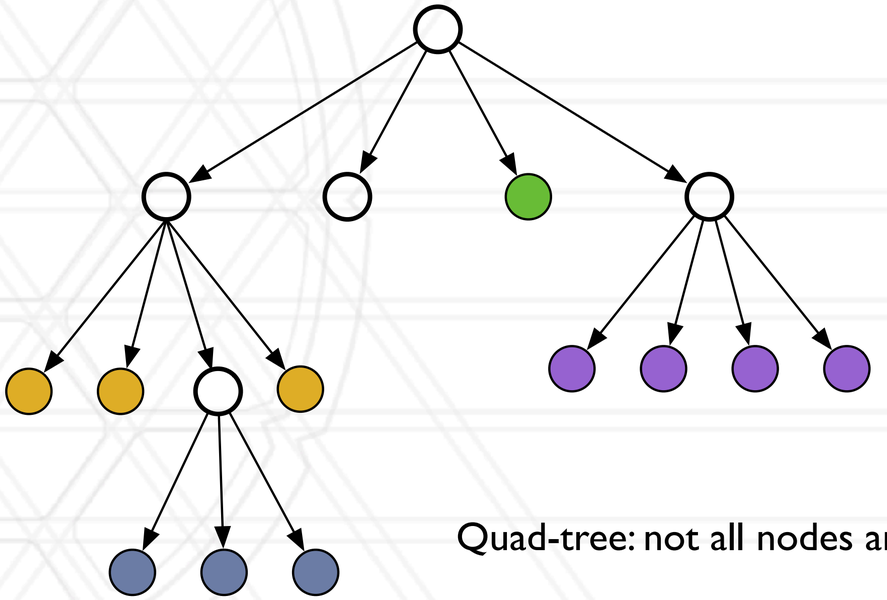

Quad-tree: not all nodes are shown

Load balance and grain size

- Load balance: try to balance the amount of work (computation) assigned to different threads/ processes
  - Bring ratio of maximum to average load as close to 1.0 as possible
  - Secondary consideration: also load balance amount of communication
- Grain size: ratio of computation-to-communication
  - Coarse-grained (more computation) vs. fine-grained (more communication)

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