

CMSC 330, Fall 2017 Quiz 4

Instructions

- Do not start this quiz until you are told to do so.
 - You have 15 minutes for this quiz.
 - This is a closed book quiz. No notes or other aids are allowed.
 - For partial credit, show all your work and clearly indicate your answers.

1. (4 points) Using the rules given below, show: $(1 + 2) + 3 \Rightarrow 6$

$$\frac{n \Rightarrow n}{\frac{e_1 \Rightarrow n_1 \quad e_2 \Rightarrow n_2 \quad n_3 \text{ is } n_1 + n_2}{e_1 + e_2 \Rightarrow n_3}}$$

$$\begin{array}{c}
 1 \Rightarrow 1 \quad 2 \Rightarrow 2 \quad 3 \text{ is } 1 + 2 \\
 \hline
 1 + 2 \Rightarrow 3 \qquad\qquad\qquad 3 \Rightarrow 3 \quad 6 \text{ is } 3 + 3 \\
 \hline
 (1 + 2) + 3 \Rightarrow 6
 \end{array}$$

2. (8 points) Using the rules given below, show: A ; let $x = 1$ in let $x = 2$ in $x + x \Rightarrow 4$

$$\frac{A(x) = v}{A; \ x \Rightarrow v}$$

$$\frac{A; e_1 \Rightarrow v_1 \quad A; x : v_1; e_2 \Rightarrow v_2}{A; \text{let } x = e_1 \text{ in } e_2 \Rightarrow v_2} \quad \frac{A; e_1 \Rightarrow n_1 \quad A; e_2 \Rightarrow n_2 \quad n_3 \text{ is } n_1 + n_2}{A; e_1 + e_2 \Rightarrow n_3}$$

$A; 1 \Rightarrow 1$	$\frac{A, x : 1; \ let\ x = 1\ in\ x + x \Rightarrow 4}{A; \ let\ x = 1\ in\ let\ x = 2\ in\ x + x \Rightarrow 4}$
$A; 1 \Rightarrow 1$	$\frac{\frac{A, x : 1; \ 2 \Rightarrow 2}{A, x : 1; \ let\ x = 2\ in\ x + x \Rightarrow 4} \quad \frac{\frac{A, x : 1; \ x : 2(x) = 2}{A, x : 1, x : 2; \ x \Rightarrow 2} \quad \frac{A, x : 1; \ x : 2(x) = 2}{A, x : 1, x : 2; \ x \Rightarrow 2}}{x + x \Rightarrow 4} \quad 4 \ is \ 2 + 2$

3. (8 points) Translate the following rules into English and describe the operation *myst* represents.

$$\text{Mystery(1): } \frac{A; e_1 \Rightarrow v_1 \quad A; e_2 \Rightarrow v_2 \quad v_1 = v_2}{A; \text{myst } e_1 e_2 \Rightarrow \text{true}} \quad \text{Mystery(2): } \frac{A; e_1 \Rightarrow v_1 \quad A; e_2 \Rightarrow v_2 \quad v_1 \neq v_2}{A; \text{myst } e_1 e_2 \Rightarrow \text{false}}$$

- Mystery(1):

Assuming e_1 evaluates to v_1 and e_2 evaluates to v_2 and v_1 equals v_2 then
 $\text{myst } e_1 e_2$ evaluates to *true*

- Mystery(2):

Assuming e_1 evaluates to v_1 and e_2 evaluates to v_2 and v_1 does not equal v_2 then
 $\text{myst } e_1 e_2$ evaluates to *false*

- Operation: The *myst* represents an equality operation.