## CMSC330 Fall 2017 Final Exam

## Name (PRINT YOUR NAME IN ALL CAPS ):

Discussion Time (circle one) $\quad 10 \mathrm{am}$ 11am 12pm $1 \mathrm{pm} \quad 2 \mathrm{pm}$ 3pm
Discussion TA (circle one) JT Greg Justin Michael BT Daniel David Derek
Cameron Eric Kesha Shriraj Pei-Jo Michael Bryan Kameron

## Instructions

- The exam has 17 pages (front and back); make sure you have them all.
- Do not start this test until you are told to do so!
- You have 120 minutes to take this exam.
- This exam has a total of 130 points, so allocate 55 seconds for each point.
- This is a closed book exam. No notes or other aids are allowed.
- Answer essay questions concisely in 2-3 sentences. Longer answers are not needed.
- For partial credit, show all of your work and clearly indicate your answers.
- Write neatly. Credit cannot be given for illegible answers.

| $\#$ | Problem | Score |
| :--- | :--- | :--- |
| 1 | PL Concepts | $/ 10$ |
| 2 | Lambda Calculus | $/ 10$ |
| 3 | OCaml Typing | $/ 10$ |
| 4 | OCaml Execution | $/ 10$ |
| 5 | OCaml Programming | $/ 12$ |
| 6 | Ruby | $/ 16$ |
| 7 | Prolog | $/ 20$ |
| 8 | Regexps, FAs, CFGs | $/ 18$ |
| 9 | Parsing | $/ 8$ |
| 10 | Operational Semantics | $/ 6$ |
| 11 | Security | $/ 10$ |
|  | TOTAL | $/ 130$ |

## 1 PL Concepts [10 pts]

1. [8 pts] Circle True or False for each of the following statements (1 point each)
2. True / False Structural ("deep") equality implies physical equality
3. True / False In Prolog, green cuts can be used to eliminate redundant computations
4. True / False Static type checking occurs during run time in OCaml
5. True / False Both Ruby and OCaml have type inference
6. True / False In SmallC, the lexing stage outputs an abstract syntax tree
7. True / False Mark and sweep garbage collection can collect cyclic data structures
8. True / False In general, static type systems are sound and complete
9. True / False In lambda calculus, some beta reductions may never terminate
10. [2 pts] Fill in the blank

A $\qquad$ in OCaml can be used to hide the implementation details of a module.

## 2 Lambda Calculus [10 pts]

1. [ $\mathbf{2} \mathbf{p t s}$ ] Make the parentheses explicit in the following expression

$$
\text { ( } \quad \lambda x . \quad y \quad x \quad y \quad \lambda a . \quad a \quad b \quad)
$$

2. [3 pts] Beta reduce the following expression until it reaches normal form. Show each step of the reduction.

$$
(\lambda x \cdot \lambda y \cdot x y)(\lambda y \cdot y) \quad x \quad(t a)
$$

3. [5 pts] Here are the Church encodings for boolean conditionals:

| true | $\lambda x . \lambda y \cdot x$ |
| :--- | :--- |
| false | $\lambda x \cdot \lambda y \cdot y$ |
| if a then b else c | a b c |

Give the lambda calculus encoding of the boolean "or" function. For example, or true false should reduce to true, and or false false should reduce to false. To make it more clear, do not substitute true, false with their lambda encodings. (hint: your answer should look like or $=\lambda \mathrm{a} . \lambda \mathrm{b}$. some appLication of a and b here)

## 3 OCaml Types [10 pts]

1. Write the types of the following OCaml expressions or write "type error" if the expression has no type:
1) $[2 \mathrm{pts}]$
[("I", 4.0); ("R", 0.0); ("S",1)]

## 2) $[2 \mathrm{pts}]$

```
fun a -> fun b -> (a b) + 1
```

2. Provide expressions (without type annotations) that have the following types:
1) $[3 \mathrm{pts}]$
```
int -> int list -> bool list
```

2) $[3 \mathrm{pts}]$
('a->'b) -> ('c->'a) -> 'c -> 'b

## 4 OCaml Execution

```
Code for map and fold is provided for reference:
let rec map f l = match l with
    [] -> []
    | h::t -> let r = f h in r :: map f t;;
let rec fold f a l = match l with
    [] -> a
    |h::t -> fold f (f a h) t ;;
```

What is the output of the following OCaml expressions?

1. [3 pts]
fold (fun a $x$-> if $x \bmod 2=0$ then a else $x:: a)$ [] [1; 2; 3; 4; 5];

## 2. [3 pts]

type taxpayer $=$ Person of float
|Company of float; ;
let $\operatorname{tax} \mathrm{y}=$
let income_tax a x = a *. x in
match y with
|Person i -> income_tax i 0.1
|Company j -> income_tax j 0.2
in
(tax (Person 100.0), tax (Company 200.0));

## 3. [4 pts]

let $f=$
let c = ref 0 in
fun a $x$-> c:= x+a; !c in
fold f 0 [1;2;3];

## 5 OCaml Programming [12 pts]

A matrix is a two-dimensional list of floats defined as:

```
type row = float list
type matrix = row list
```

1. [6 pts] Write a function that, given matrix $m$ and ints $i$ and $j$, returns the element at row $i$ and column $j$. If $i$ or $j$ is out of bounds, return None. For example:
```
let m = [[1.0 ; 2.0]; [3.5 ; 4.5]] in
get_element m 0 0 T Some 1.0
get_element m 0 1 }->\mathrm{ Some 2.0
get_element m 1 0 T Some 3.5
get_element m 3 0 -> None
```

Write your answer below. (Hint: Write a helper function to get an element at an index from a list).
let rec get_element (m : matrix) (i : int) (j : int) : float option =
2. [6 pts] Write a function that, given float $c$ and matrix $m$, returns a new matrix with elements in $m$ multiplied by c .

```
let m = [[1.0 ; 2.0] ; [3.5 ; 4.5]] in
scalar_mult m 0.0 -> [[0.0 ; 0.0] ; [0.0 ; 0.0]]
scalar_mult m 1.5 -> [[1.5 ; 3.0] ; [5.25 ; 6.75]]
```

Write your answer below. (Hint: You know a higher-order function that makes this question very easy).

```
let rec scalar_mult (m : matrix) (c : float) : matrix =
```


## 6 Ruby [16 pts]

For this question, you need to write several methods to work with a data file containing transactions. Each line of the file has three columns: date, amount, and location. Date is in YYYY-MM-DD format, amount is a decimal with two digits after the point, and location is an arbitrary string. The amount does not start with a decimal point (but it can start with a zero). Each item is separated by a comma with no whitespace. Here is an example file:

$$
\begin{aligned}
& \text { 2017-11-27,-250.00, Amazon.com } \\
& \text { 2017-11-16,-9.50, Chipotle } \\
& \text { 2017-11-15, 10.00, UMD Paycheck }
\end{aligned}
$$

Write the following methods for a class Transactions:

1. [5 pts] initialize(datafile): The constructor takes as input a string containing the filename of the transactions, and it loads them into field @t of the current object. The @t field should be an array where each array element is itself an array [date, amount, location], where the first and last items are strings and the amount is a float (use String\#to_f. Example: "1234.5".to_f $\Rightarrow$ 1234.5). You must validate the formatting of the file. If the file is invalid, raise an exception (hint: use raise "Invalid Input"). You can use the following pattern to read lines from a file:
```
    IO.foreach("file") { |line| puts line }
def initialize(datafile)
```

end
2. [5 pts] get_net_growth(start_date,end_date): Returns as a float the total amount of money made (or lost) between the given start date and end date, inclusive. You may assume both dates are valid. To help you out, you may assume there is a function date_cmp(date1, date2), which will return $<0$ if date 1 is earlier than date2, 0 if they are the same date, and $>0$ if date1 is later than date2.
def get_net_growth(start_date, end_date)
end
3. [6 pts] most_frequent: Takes no arguments, and returns the location that occurs most frequently in the transaction list. If there is a tie, it does not matter which one you pick.
def most_frequent
end

## 7 Prolog [20 pts]

1. [6 pts] consider the following definitions:
job(alice, programmer).
job(bob, manager).
job(celine, ceo).
supervises(A, B) :- job(A, manager), job(B, programmer).
supervises(A, B) :- job(A, ceo), job(B, manager).
can_fire(A, B) :- supervises(A, B).
can_fire(A, B) :- supervises(A,C), can_fire(C,B)
low_level(A) :- \+ can_fire(A, _). \# \+ is the same as not
For each query, list the substitutions that Prolog produces that makes the query true.
1) ?- supervises(celine, X).
2) ?- can_fire(X, alice).
3) ?- low_level(X).
2. [4 pts] List all substitutions that satisfy the following query, or write false if no such solution exists.
?- member(X, [0, 2]), length(Q, X), append(A, Q, [1, 2, 3, 4, 5]).
3. [5 pts] Implement nim $(N, L)$, where if $N$ is a non-negative integer, then $L$ is a list of 1 s and 2s that add up to N .
?- $\operatorname{nim}(0, L)$.
L = [].
?- $\operatorname{nim}(3, L)$.
$\mathrm{L}=[1,1,1] ; \mathrm{L}=[1,2] ; \mathrm{L}=[2,1]$.
4. [5 pts] Implement merge (A, B, C), where if $A$ and $B$ are sorted lists of integers, then $C$ is the lists merged together. In other words, C is a sorted list of integers which contains all elements in both A and B. You CANNOT use the predicate sort(+List, -Sorted).
?- merge([], [], C).
C = [].
?- merge([], [1, 2], C).
$C=[1,2]$.
?- merge([1, 4], [2, 3, 5], C).
$C=[1,2,3,4,5]$.

## 8 Regexps, FAs, CFGs [18 pts]

1. [3 pts] Write a regular expression for describing all the even length strings over the alphabet $\{a, b\}$.
2. [3 pts] Construct an NFA corresponding to the regular expression (s|rs)(rr)*.
3. Consider the following NFA:

1) [ 3 pts] What regex does this NFA represent?
2) [5 pts] Convert the NFA to a DFA.
4. [4 pts] Write a context-free grammar for the language of strings over the alphabet \{a, b\} containing an equal number of a's and b's. For example, "ab", "ba", "aabb", "abab", and the empty string are in the language, but "a", "b", "aba", and "aab" are not.

## 9 Parsing [8 pts]

$S \rightarrow B S \mid C$
$\mathrm{B} \rightarrow \mathrm{aB}|\mathrm{bB}| \mathrm{cB} \mid \varepsilon$
$C \rightarrow x \mid y$

1. [3 pts] Given this CFG, calculate the first sets of $B$ and $S$ ( $\varepsilon$ represents the empty string)

$$
\begin{array}{ll}
\operatorname{First}(B)=\{ & \} \\
\operatorname{First}(S)=\{ & \}
\end{array}
$$

For the next part you are given the following utilities for parsing.
lookahead: Variable holding next terminal
match(x) : Function to match next terminal to $x$
error(): Signals a parse error
2. [5 pts] Write OCaml code for parse_S() for the CFG from part 1 using the above utilities. Assume parse_B(), and parse_C() are given. Any errors should be handled by raising an exception.

## 10 Operational Semantics [6 pts]

1. [ 3 pts ] Give a derivation showing that let $x=$ let $x=2$ in 1 in $x$ evaluates to 1 in the empty environment using the following operational semantics rules:

$$
\frac{A(x)=v}{A ; x \Rightarrow v} \quad \overline{A ; n \Rightarrow n} \quad \frac{A ; e_{1} \Rightarrow v_{1} \quad A, x_{1}: v_{1} ; e_{2} \Rightarrow v_{2}}{A ; \operatorname{let} x_{1}=e_{1} \text { in } e_{2} \Rightarrow v_{2}}
$$

2. [3 pts] Given the following rule for a while loop:

$$
\frac{A_{1} ; b_{1} \Rightarrow \text { false } A_{1} ; s_{1} \Rightarrow A_{2}}{A_{1} ; \text { while } b_{1} \text { do } s_{1} \Rightarrow A_{2}} \quad \begin{aligned}
& A_{1} ; b_{1} \Rightarrow \text { true } A_{1} ; s_{1} \Rightarrow A_{2} \\
& A_{2} ; \text { while } b_{1} \text { do } s_{1} \Rightarrow A_{3} \\
& A_{1} ; \text { while } b_{1} \text { do } s_{1} \Rightarrow A_{3}
\end{aligned}
$$

What unexpected behavior for while will the resulting language have?

## 11 Security [10 pts]

Multiple choice questions [1 point each]

1. What should you do to validate user input?
a. Reject the input with unwanted characters
b. Escape unwanted characters
c. Remove unwanted characters
d. All of the above
2. What is the security benefit of using prepared statements?
a. They ensure user data is parsed as input, not code
b. User data will always be encrypted
c. They make constructing queries easier
d. They prevent server-side errors
3. Consider the following code:
```
def sanitize_input(userString)
    reg = /[-\/\\^$*+?.()@|{}]/
    return userString.gsub(reg, '')
end
```

(Hint: gsub(pattern, replacement) returns a string where all occurrences of pattern are substituted for the second argument.)

This snippet is an example of validating user input by
a. Whitelisting
b. Blacklisting
c. Escaping characters
d. XSS prevention
4. A stored XSS attack typically must be prevented by
a. The user's web browser
b. A network administrator
c. The database executing SQL code
d. The web server
5. The following is a function used in a very buggy Ruby file transfer application.

```
def get_directory_contents(directory, userName)
    if !directory.include?(userName) then
                return nil
    else
                return `ls #{directory}` # executes shell command
        end
end
```

1) [1 pts] In THREE WORDS OR FEWER, name a vulnerability that exists in the above code
2) [ $\mathbf{2} \mathbf{~ p t s ] ~ G i v e ~ a n ~ e x a m p l e ~ o f ~ a ~ v a l u e ~ f o r ~ t h e ~ d i r e c t o r y ~ p a r a m e t e r ~ t h a t ~ e x p l o i t s ~ y o u r ~}$ given vulnerability:
3) [ 3 pts] Write a short code that fixes the vulnerability while maintaining intended functionality. Indicate at which line you want to insert your code.
